

SECTION-II

(Numerical Value Answer Type)

This section contains 5 questions. The answer to each question is a Numerical values comprising of positive or negative decimal numbers.

Marking Scheme: +4 for correct answer, 0 in all other cases.

21. If $[\bar{a} \times \bar{b} \bar{b} \times \bar{c} \bar{c} \times \bar{a}] = \lambda [\bar{a} \bar{b}, \bar{c}]^2$ then $\lambda =$
22. Let \bar{u} be a vector coplanar with the vectors $\bar{a} = 2\bar{i} + 3\bar{j} - \bar{k}$, $\bar{b} = \bar{j} + \bar{k}$. If \bar{u} is perpendicular to \bar{a} and $\bar{u} \cdot \bar{b} = 24$ then $|\bar{u}|^2 =$
23. $A = (2, 3, 5)$, $B = (-1, 3, 2)$ and $C(\lambda, 5, \mu)$ are the vertices of a triangle. If the median \overline{Am} is Equally inclined to the coordinate axes then $\lambda =$
24. In the ΔABC if $A = (-2, 3, 4)$ and the mid points of BC, CA, AB are $(1, -4, 2)$, $(-5, 2, -3)$, F respectively then $F_x + F_z =$ _____
25. If the plane $2x - 3y + 5z - 2 = 0$ divides the line segment joining the points $(1, 2, 3)$ and $(2, 1, k)$ in 9:1 then $k =$ _____

PHYSICS

SECTION-I

(SINGLE CORRECT ANSWER TYPE)

This section contains 20 multiple choice questions. Each question has 4 options (1), (2), (3) and (4) for its answer, out of which ONLY ONE option can be correct.

Marking Scheme: +4 for correct answer, 0 if not attempted and -1 if not correct

SYLLABUS: ELECTRICITY

26. The average current is a sinusoidally varying a.c of peak value 5A with initial phase zero, between the instants $t = \frac{T}{8}$ to $t = \frac{T}{4}$ is.

1) $\frac{10}{\pi} \sqrt{2} A$	2) $\frac{5}{\pi} \sqrt{2} A$	3) $\frac{20}{\pi} \sqrt{2} A$	4) $\frac{10}{\pi} A$
--------------------------------	-------------------------------	--------------------------------	-----------------------
27. A circuit operating at $\frac{360}{2\pi} Hz$ contains $1\mu F$ capacitor and 20Ω resistor. The inductor must be added in series to make the phase angle for the circuit zero is

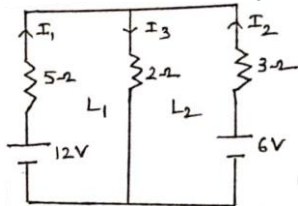
1) $9H$	2) $7.7H$	3) $14H$	4) $18H$
---------	-----------	----------	----------
28. A $8\mu F$ capacitor is connected across 220V and 50Hz line. The peak value of charge through the capacitor is

1) $2.5 \times 10^{-4} C$	2) $5 \times 10^{-5} C$	3) $2.5 \times 10^{-3} C$	4) $7.5 \times 10^{-2} C$
---------------------------	-------------------------	---------------------------	---------------------------
29. A coil of resistance 20Ω and inductance $0.5H$ is switched to dc 200V supply. Calculate the rate of increase in current at the instants of closing the switch.

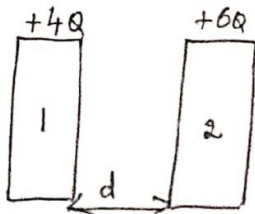
1) $200 A/s$	2) $300 A/s$	3) $100 A/s$	4) $400 A/s$
--------------	--------------	--------------	--------------
30. A square of side 'L' meter lies in the XY-plane in a region where the magnetic field is given by $\vec{B} = B_0 (2\hat{i} + 3\hat{j} + 4\hat{k})T$, ' B_0 ' is constant. Find the magnetic flux passing through the square (in wb)

1) $4B_0L^2$	2) $2B_0L^2$	3) $3B_0L^2$	4) B_0L^2
--------------	--------------	--------------	-------------

31. Calculate the maximum power induced in the coil of 100 turns of 0.01m^2 area rotating at the rate of 50 rps about an axis perpendicular to uniform magnetic field of 0.05T . The resistance of the coil is 30Ω
- 1) 4.23 w 2) 8.03 w 3) 8.23 w 4) 8.52 w
32. A proton is projected with a velocity of 10^7 m/s at right angles to uniform magnetic field by induction 100 mT . The time taken by proton to traverse 60° arc is.
- 1) $0.81 \times 10^{-7}\text{ s}$ 2) $1.05 \times 10^{-7}\text{ s}$ 3) $1.62 \times 10^{-7}\text{ s}$ 4) $3.34 \times 10^{-7}\text{ s}$
33. The instantaneous acceleration of an electron in a magnetic field $\vec{B} = 2\hat{i} + 3\hat{j} + 4\hat{k}$ is $\vec{a} = x\hat{i} + \hat{j} - \hat{k}$. The magnitude of acceleration is (ms^{-1})
- 1) 1.5 2) $\sqrt{1.5}$ 3) 0.5 4) $\sqrt{2.5}$
34. A charge 'q' move with a velocity 2ms^{-1} along x-axis in a uniform magnetic field $\vec{B} = \hat{i} + 2\hat{j} + 3\hat{k}$ T, charge experiences force in
- 1) X-Y Plane 2) along Y axis 3) along Z axis 4) Z-Y Plane
35. A current 1A flows downwards in a long straight vertical conductor and the earths horizontal magnetic field is $5 \times 10^{-7}\text{T}$, then the neutral point occurs
- 1) due north 10cm from the wire 2) due east 10cm from the wire
3) due east 0.4cm from the wire 4) due west 5cm from the wire
36. A battery is connected to resistance of 10Ω the current in the circuit is 0.12 A . The same battery gives 0.07A current with 20Ω . Find the emf of the battery
- 1) 1.5 v 2) 1.68 v 3) 1.8 v 4) 1.78 v
37. Find the value of I_3

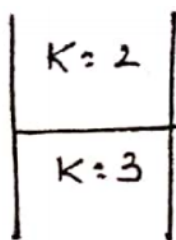


- 1) 2.129 A 2) 3.2 A 3) 3.219 A 4) 4.62 A
38. In a potentiometer experiment the balancing length a cell is 560 cm . When an external resistance is connected in parallel to the cell the balancing length changes by 60cm . If the internal resistance of the cell is 1.2Ω . Find the external resistance.
- 1) 10Ω . 2) 20Ω . 3) 30Ω . 4) 40Ω .
39. If the length of the filament of a heater is reduced by 10% the power of the heater will be
- 1) 12% 2) 11% 3) 13% 4) 14%
40. Two similar conducting plates are placed at a distance of 'd' as shown in the figure. What is potential difference between them



- 1) $\frac{Qd}{A\epsilon_0}$ 2) $\frac{5Qd}{A\epsilon_0}$ 3) $\frac{-Qd}{A\epsilon_0}$ 4) $\frac{-5Qd}{A\epsilon_0}$
41. Three point charges are arranged as shown in the figure. Find the position of the charges such that P.E of the system is minimum (in cm)
-
- 1) $3,10,0$ 2) $0,3,8$ 3) $0,9,3$ 4) $0,3,9$

42. A parallel plate capacitor with air as the medium has a capacitance of $0.5\mu F$. Half of its space is filled with a dielectric of $k = 2$ and the other half is filled with a dielectric of $k = 3$. Find its net capacity (in μF)



- 1) 2.5 2) 3.125 3) 2.6 4) 1.25
43. Semi circular ring of radius 0.5 m is uniformly charged with a total charge of $1.4 \times 10^{-19} C$. The electric field intensity at the centre of the ring is (in V/m)
- 1) 12 2) 16 3) 32 4) 30
44. Find the net electric dipole moment of the system of charges as shown in the figure
- 1) $\frac{ql}{\sqrt{2}}(\hat{i} + \hat{j})$ 2) $-\sqrt{3}q\hat{j}$ 3) $\sqrt{3}ql\hat{j}$ 4) $2ql\hat{j}$
45. An electron initially at rest falls at a distance of 1.5 m in a uniform electric field of magnitude $2 \times 10^4 N/c$. The time taken by the electron to fall this distance is (in sec)
- 1) 2.9×10^{-9} 2) 1.3×10^{-2} 3) 1.6×10^{-10} 4) 2.1×10^{-12}

SECTION-II

(Numerical Value Answer Type)

This section contains 5 questions. The answer to each question is a Numerical values comprising of positive or negative decimal numbers.

Marking Scheme: +4 for correct answer, 0 in all other cases.

46. The bob of a simple pendulum has mass of 40g and a positive charge $4 \times 10^{-6} C$. It makes 20 oscillations in 45 sec. A vertical electric field pointing upward and a magnitude $2.5 \times 10^4 N/C$ is switched on. How much time will it take for 20 oscillations ____
47. An electric field $\vec{E} = 10x\hat{i} + 30y\hat{j} + 40z\hat{k} N/C$ exists in the space. Take the potential at (0,0,0) to be zero, find the potential at (1m, 2m, 3m). ____
48. In a meter bridge, the null point is found at a distance of 33.7 cm from 'A'. If a resistance of 12Ω is connected in parallel with 's' the null point occurs at 51.9 cm. Find the value of 's' ____
49. A charged particle of charge 4 milli coulomb enters uniform magnetic field $\vec{B} = 3\hat{i} + 6\hat{j} + 6\hat{k} T$ with a velocity $\vec{V} = 4\hat{i} - x\hat{j} + y\hat{k}$. If the particle moves undeviated find the magnitude of its velocity. ____
50. The magnetic flux through a coil perpendicular to the plane is varying according to the relation $\phi = (5t^3 + 4t^2 + 2t - 5) wb$. If the resistance of the coil is 5Ω , find the induced current in it at $t = 2sec$ ____

CHEMISTRY
SECTION-I

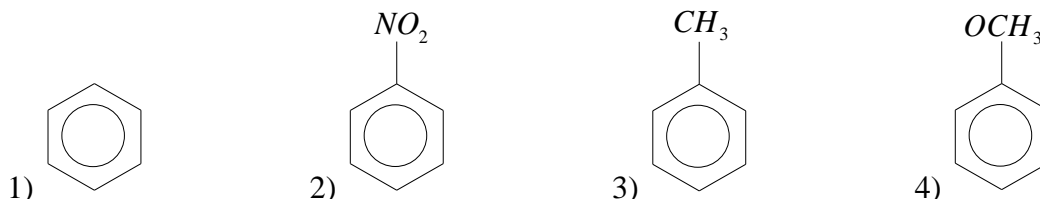
(SINGLE CORRECT ANSWER TYPE)

This section contains 20 multiple choice questions. Each question has 4 options (1), (2), (3) and (4) for its answer, out of which ONLY ONE option can be correct.

Marking Scheme: +4 for correct answer, 0 if not attempted and -1 if not correct

SYLLABUS: FIRST YEAR ORGANIC CHEMISTRY

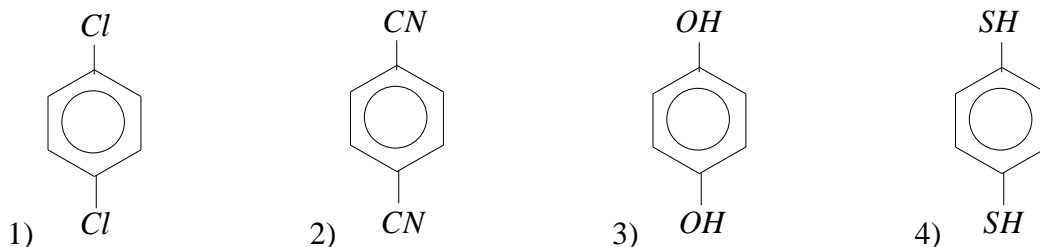
51. Which of the following will have fastest rate of reaction with $Br_2 / FeBr_3$



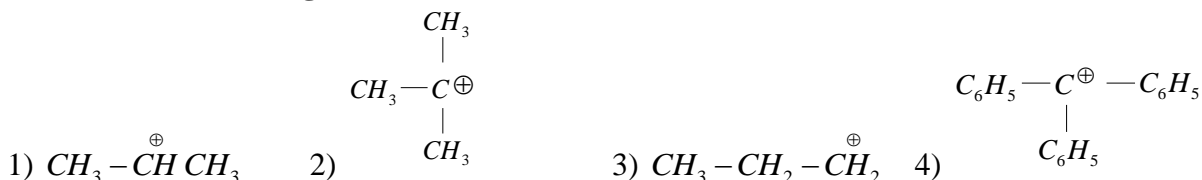
52. Geometrical Isomerism is possible in



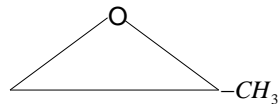
53. Which of the following molecule significant $\mu \neq 0$.



54. Which of the following is most stable cation.



55. The IUPAC name of the compound



- 1) propylene oxide 2) 1,2-oxopropane 3) 1,2 - epoxy propane 4) 1,2 - prop oxide

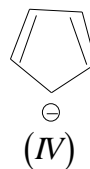
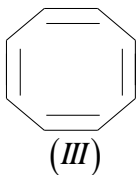
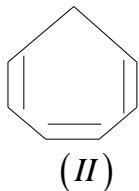
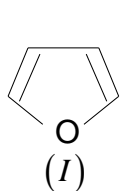
56. 2,3 - pentadiene exhibits optical Isomerism since it.

- 1) contains one chiral carbon
2) contains two chiral carbons
3) does not contains any chiral carbon but molecule as a whole is chiral
4) does not exhibits optical isomerism

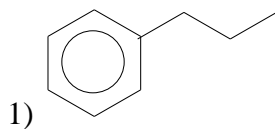
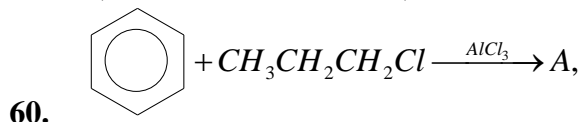
57. The major product obtained in the photobromination of 2-methyl butane is

- 1) 1-bromo-2-methyl butane 2) 1-bromo-3-methyl butane
3) 2-bromo-3-methyl butane 4) 2-bromo-2-methyl butane

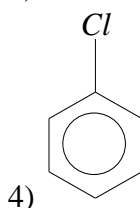
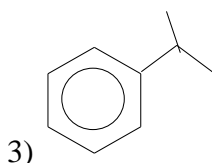
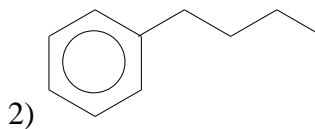
58. Which of the following compounds are Anti-Aromatic



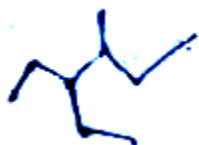
59. $B \xleftarrow[\text{Catalyst}]{\text{Lindlar's}} R-C \equiv C-R \xrightarrow{\text{Na/Liq.NH}_3} A$
- 1) A-trans, B-cis 2) A-cis, B-trans 3) A,B are cis 4) A, B are trans



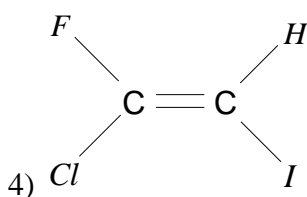
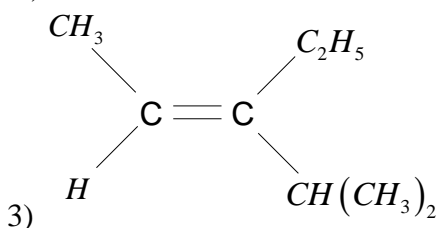
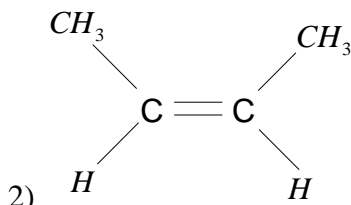
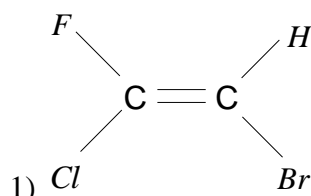
what is A.



61. $CH \equiv CH + NaNH_2 \rightarrow A \xrightarrow[CH_3Cl]{2\text{ moles}} B$, then B is
- 1) 1-Butyne 2) 2-Butyne 3) 2-pentyne 4) propyne.
62. $C_2H_6 \xrightarrow{450^\circ C} A \xrightarrow{S_2Cl_2} B$, then B is
- 1) $(C_2H_5)_2S$ 2) $(C_2H_4Cl)_2S$ 3) $(CH_3Cl)_2S$ 4) $(CH_3)_2S$
63. The compound which is not purified by sublimation is
- 1) phenol 2) benzoic acid 3) camphor 4) naphthalene
64. In allene (C_3H_4), the type of hybridization of the carbon atoms is
- 1) Sp, Sp^2 2) Sp, Sp^3 3) only Sp^2 4) Sp^2, Sp^3
65. The IUPAC name of the following compound is



- 1) 3,4-diethyl hexane 2) 4-ethyl-3 methyl hexane
3) 4-methyl-3-ethyl hexane 4) 3-ethyl-4-methyl hexane
66. The 'E' isomer is



KEY SHEET

MATHS

1) 4	2) 4	3) 3	4) 3	5) 2	6) 3	7) 2	8) 1	9) 2	10) 4
11) 2	12) 4	13) 1	14) 3	15) 3	16) 1	17) 1	18) 1	19) 4	20) 3
21) 1	22) 336	23) 7	24) 13	25) 0					

PHYSICS

1) 1	2) 2	3) 3	4) 4	5) 1	6) 3	7) 2	8) 1	9) 4	10) 3
11) 2	12) 1	13) 1	14) 2	15) 3	16) 4	17) 4	18) 3	19) 2	20) 1
21) 52	22) -245	23) 13.47	24) 12	25) 15.6A					

CHEMISTRY

1) 4	2) 4	3) 1	4) 4	5) 2	6) 3	7) 4	8) 1	9) 1	10) 3
11) 2	12) 2	13) 1	14) 1	15) 4	16) 3	17) 2	18) 1	19) 3	20) 1
21) 3	22) 4	23) 23.7	24) 3	25) 4					

HINTS & SOLUTIONS

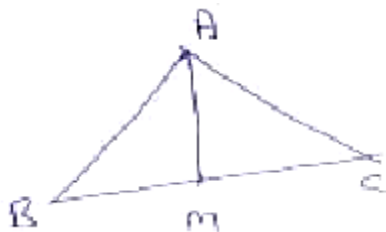
MATHEMATICS

1.
$$\overline{OG} = \frac{\overline{OA} + \overline{OB} + \overline{OC}}{3}, \overline{OG}^1 = \frac{\overline{OA}^1 + \overline{OB}^1 + \overline{OC}^1}{3}$$

$$AA^1 + BB^1 + CC^1 = \overline{OA}^1 + \overline{OB}^1 + \overline{OC}^1 - (\overline{OA} + \overline{OB} + \overline{OC})$$

$$= 3\overline{OG}^1 - 3\overline{OG}$$

$$= 3\overline{GG}^1$$



2.
$$\overline{Bm} = \frac{1}{2}\overline{Bc} = \frac{1}{2}(-\bar{i} - 2\bar{k})$$

$$\overline{Am} = \overline{AB} + \overline{Bm} = -3\bar{i} + 4\bar{k} - \frac{1}{2}\bar{i} - \bar{k}$$

$$= \frac{-7\bar{i}}{2} + 3\bar{k}$$

$$|\overline{Am}| = \sqrt{\frac{49}{4} + 9} = \frac{\sqrt{85}}{2}$$

$$3. \quad \overline{AC} = \overline{a} + \overline{b} = 3\overline{i} + 6\overline{j} - 2\overline{k}$$

$$\overline{BD} = \overline{b} - \overline{a} = -\overline{i} - 2\overline{j} - 2\overline{k}$$

$$|\overline{AC}| = \sqrt{9+36+4} = 7$$

$$|\overline{BD}| = \sqrt{1+4+4} = 3.$$

$$4. \quad |\overline{a} + \overline{b} + \overline{c}|^2 > 0$$

$$1+1+1+2(\overline{a}.\overline{b} + \overline{b}.\overline{c} + \overline{c}.\overline{a}) > 0$$

$$\Rightarrow \overline{a}.\overline{b} + \overline{b}.\overline{c} + \overline{c}.\overline{a} > \frac{-3}{2} \text{ --- (1)}$$

$$\max k = |\overline{a} - \overline{b}|^2 + |\overline{b} - \overline{c}|^2 + |\overline{c} - \overline{a}|^2$$

$$= 2(1+1+1) - 2(\overline{a}.\overline{b} + \overline{b}.\overline{c} + \overline{c}.\overline{a})$$

$$= 6 - 2\left(\frac{-3}{2}\right) = 9$$

$$k \left[2|\overline{a}|^2 + 3|\overline{b}|^2 - 4|\overline{c}|^2 \right] = 9(2+3-4) = 9$$

$$5. \quad \overline{OP}.\overline{i} = 1 \quad \overline{OQ}.\overline{i} = -1$$

$$x_1 = 1 \quad x_2 = -1$$

$$y_1 = 5 \quad y_2 = -1$$

$$P = (1, 5) \quad Q = (-1, -1)$$

$$|2\overline{OP} + 3\overline{OQ}| = |-i + 7j| = \sqrt{50} = 5\sqrt{2}$$

6.

$$\overline{b}.\overline{c} + \overline{a}.\overline{r} = \overline{c}.\overline{a} + \overline{b}.\overline{r}$$

$$(\overline{b} - \overline{a}).\overline{c} = (\overline{b} - \overline{a}).\overline{r}$$

$$(\overline{b} - \overline{a}).(\overline{c} - \overline{r}) = 0$$

$$\overline{AB}.\overline{PC} = 0$$

$$\text{Similarly } \overline{BC}.\overline{PC} = 0$$

P is Ortho Centre



$$7. \quad \overline{BC} = \overline{BA} + \overline{AC} = -\overline{b} + \overline{c}$$

$$Am = \frac{|\overline{BA} \times \overline{BC}|}{|\overline{BC}|} = \frac{|-\overline{b} \times (-\overline{b} + \overline{c})|}{|-\overline{b} + \overline{c}|} = \frac{|\overline{b} \times \overline{c}|}{|\overline{b} - \overline{c}|}$$

$$8. \quad \text{Normal vector of OPQ is } \overline{op} \times \overline{oq}$$

$$= \begin{vmatrix} i & j & k \\ 1 & -1 & 2 \\ -2 & -1 & 1 \end{vmatrix} = \overline{i} - 5\overline{j} - 3\overline{k}$$

$$\cos \theta = \frac{5+5+9}{\sqrt{35}.\sqrt{35}} = \frac{19}{35}$$

$$\theta = \cos^{-1}\left(\frac{19}{35}\right)$$

9. $\bar{a} \cdot (\bar{a} + \bar{b} + \bar{c}) = 1$

$$p[\bar{a}\bar{b}\bar{c}] + q[\bar{c}\bar{a}\bar{b}] + r[\bar{a}\bar{b}\bar{c}] = 1$$

$$[\bar{a}\bar{b}\bar{c}] = \frac{1}{p+q+r}$$

10.
$$\begin{vmatrix} a & 1 & 1 \\ 1 & b & 1 \\ 1 & 1 & c \end{vmatrix} = 0$$

$$R_2 \rightarrow R_2 - R_1$$

$$R_3 \rightarrow R_3 - R_1$$

$$\begin{vmatrix} a & 1 & 1 \\ 1-a & b-1 & 0 \\ 1-a & 0 & c-1 \end{vmatrix} = 0$$

$$a(b-1)(c-1) - 1(1-a)(c-1) - (1-a)(b-1) = 0$$

$$\frac{a}{1-a} + \frac{1}{(1-b)} + \frac{1}{(1-c)} = 0$$

$$1 + \frac{a}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 1$$

11. \overline{AB} divides yz plane in the ratio $-x_1 : x_2$

$$\left(0, \frac{13}{2}, \frac{-13}{2}\right) = \left(\frac{-15+15}{-5+3}, \frac{-5b+3}{-5+3}, \frac{-5+3a}{-5+3}\right)$$

$$\frac{-5b+3}{-2} = \frac{17}{2} \Rightarrow -5b+3 = -17$$

$$\Rightarrow -5b = -20$$

$$\Rightarrow b = 4$$

$$\frac{-13}{2} = \frac{-5+3a}{-2} \Rightarrow 3 = -5+3a$$

$$\Rightarrow a = \frac{18}{3} = 6$$

12. $l^2 + m^2 + n^2 = k$, range of $lm + mb + nl$ is

$$\left[\frac{-k}{2}, k\right]$$

13. $m = \sqrt{(x_2 - x_1)^2 + (z_2 - z_1)^2}$

$$= \sqrt{(-1-3)^2 + (1+2)^2}$$

$$= \sqrt{16+9} = 5$$

$$l = |y_2 - y_1| = |0-1| = 1$$

$$3l^2 - m + 1 = 3(1)^2 - 5 + 1 = -1$$

14. $P = (1, 3, 4)$

$$\pi = 2x - y + z + 3 = 0$$

$$\frac{h-1}{2} = \frac{k-3}{-1} = \frac{l-4}{1} = -2 \frac{(2-3+4+3)}{4+1+1}$$

$$\frac{h-1}{2} = \frac{k-3}{-1} = \frac{l-4}{1} = -2(1)$$

$$h = -3, k = 5, l = 2$$

15. $A = \text{Foot of } \perp r \text{ from } P \text{ to } x + y + z = 3$

$$\frac{h-0}{1} = \frac{k-1}{1} = \frac{l-0}{1} = \frac{-(0+1+0-3)}{1+1+1}$$

$$\frac{h}{1} = k-1 = z = \frac{2}{3}$$

$$h = \left(\frac{2}{3}, \frac{5}{3}, \frac{2}{3} \right)$$

$B = \text{Foot of the } \perp r \text{ from } Q \text{ to } x + y + z = 3$

$$\frac{h-0}{1} = \frac{k-0}{1} = \frac{l-1}{1} = \frac{-(0+1+0-3)}{1+1+1}$$

$$h = \frac{2}{3}, k = \frac{2}{3}, l = \frac{5}{3}$$

$$AB = \sqrt{0+1+1} = \sqrt{2}$$

16. $\left(\frac{a}{3}, \frac{b}{3}, \frac{c}{3} \right) = (x_1, y_1, z_1)$

$$a = 3x_1, b = 3y_1, c = 3z_1$$

$$3P = \sqrt{\frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2}}$$

$$3P = \frac{|-1|}{\sqrt{\frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2}}}$$

$$\Rightarrow \frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2} = \frac{1}{9P^2}$$

$$\Rightarrow \frac{1}{9x_1^2} + \frac{1}{9y_1^2} + \frac{1}{9z_1^2} = \frac{1}{9P^2}$$

$$\therefore \text{Locus of 'P' is } \frac{1}{x^2} + \frac{1}{y^2} + \frac{1}{z^2} = \frac{1}{P^2}$$

17. Put $\frac{x+1}{3} = \frac{y-2}{-2} = \frac{z+1}{-1} = r$

$$P = (3r-1, -2r+2, -r-1)$$

$$A = (1, 0, 2)$$

$$d'rs \text{ of } \overline{AP} = (3r-2, -2r+2, -r-3)$$

$$\overline{AP} \perp r \quad L = 0$$

$$\Rightarrow (3r-2)3 + (-2r+2) - 2 + (-r-3)(-1) = 0$$

$$\Rightarrow 9r - 6 + 4r - 4 + r + 3 = 0$$

$$14r - 7 = 0 \Rightarrow r = \frac{1}{2}$$

$$\text{d.r.'s } \overline{AP} \text{ are } \left(\frac{-1}{2}, 1, \frac{-7}{2} \right)$$

$$\Rightarrow \frac{x-1}{1} = \frac{y-2}{-2} = \frac{z-3}{7}$$

18. $\frac{x-2}{3} = t \Rightarrow x = 3t + 2$

$$\frac{y+1}{4} = t \Rightarrow y = 4t - 1$$

$$\frac{z-1}{12} = t \Rightarrow z = 12t + 2$$

Substitute

$$x - y + z = 5 \Rightarrow t = 0 \Rightarrow x = 2, y = -1, z = 2$$

$$Q = (2, -1, 2), P = (-1, -5, -10)$$

19. $\frac{x-4}{1} = \frac{y-2}{1} = \frac{z-\lambda}{3} = r_1$

$$x = r_1 + 4, y = r_1 + 2, z = 3r_1 + \lambda$$

$$\frac{x}{1} = \frac{y+2}{2} = \frac{z}{4} = r_2$$

$$x = r_2, y = 2r_2 - 2, z = 4r_2$$

\therefore both the lines intersect

$$(r_1 + 4, r_1 + 2, 3r_1 + \lambda) = (r_2, 2r_2 - 2, 4r_2)$$

Compare both sides and solve it

We get

$$r_1 = -4, r_2 = 0$$

$$\therefore \lambda = 12$$

20. Take the Mid-Point of P and Q and substitute in $2x - y + z + 3 = 0$

Numerical Value Questions:-

21. $[\bar{a} \times \bar{b} \ \bar{b} \times \bar{c} \ \bar{c} \times \bar{a}] = \lambda [\bar{a} \ \bar{b} \ \bar{c}]^2$

$$[\bar{a} \ \bar{b} \ \bar{c}]^2 = \lambda [\bar{a} \ \bar{b} \ \bar{c}]^2 = \lambda = 1$$

22. $\bar{\mu} = x\bar{a} + y\bar{b}$

$$\bar{\mu} \cdot \bar{a} = 0 \Rightarrow 7x + y = 0$$

$$\bar{\mu} \cdot \bar{b} = 24 \Rightarrow x + y = 12$$

$$x = -2, y = 14$$

$$\bar{\mu} = -2\bar{a} + 14\bar{b} = 4\bar{i} + 8\bar{j} + 16\bar{k}$$

$$|\mu|^2 = 16 + 64 + 256 = 336$$

23. Mid-Point of BC is $m = \left(\frac{\lambda-1}{2}, 4, \frac{\mu+2}{2} \right)$

$$\overline{Am} = \left(\frac{\lambda-5}{2} \right) \bar{i} + \bar{j} + \left(\frac{\mu-8}{2} \right) \bar{k}$$

$$\overline{Am} \cdot \bar{i} = \overline{Am} \cdot \bar{j} = \overline{Am} \cdot \bar{k}$$

$$\frac{\lambda-5}{2} = 1 = \frac{\mu-8}{2}$$

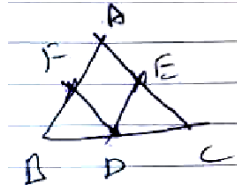
$$\lambda = 7, \mu = 10$$

24. $F_x = A + D - E$

$$F = (-2, 3, 4) + (1, -4, 2) - (-5, 2, -3)$$

$$F = (4, -3, 9)$$

$$F_x + F_z = 4 + 9 = 13$$



25. $\pi = 2x - 3y + 5z - 2 = 0$

$$A = (1, 2, 3), B(2, 1, k)$$

$$-\pi_{111} : \pi_{222} = 9 : 1$$

$$\Rightarrow - \left[\frac{2-6+15-2}{4-3+5k-2} \right] = \frac{9}{1}$$

$$\Rightarrow - \left[\frac{9}{5k-1} \right] = 9$$

$$5k - 1 = -1$$

$$5k = 0$$

$$\boxed{k = 0}$$

PHYSICS

26. $\int_{t_1}^{t_2} i dt / \int_{t_1}^{t_2} dt = i_0 \sin wt$

$$\frac{T}{4} \int_{T/8}^{T/4} 5 \sin wt dt / \int_{T/8}^{T/4} dt$$

$$= \frac{5}{w} [-\cos wt]_{T/8}^{T/4} / [t]_{T/8}^{T/4}$$

$$= \frac{-5 \left[\cos \frac{2\pi}{T} \times \frac{T}{4} - \cos \frac{2\pi}{T} \times \frac{T}{8} \right]}{\frac{2\pi}{T} \left(\frac{T}{4} - \frac{T}{8} \right)}$$

$$= \frac{5}{\sqrt{2}} / \frac{\pi}{4} = \frac{10\sqrt{2}}{\pi}$$

$$27. \quad \cos \phi = \frac{R}{Z} \quad \phi = 0^\circ \Rightarrow \cos \phi = 1$$

$$\Rightarrow R = Z$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$Z^2 = R^2 + (X_L - X_C)^2$$

$$R^2 = R^2 + (X_L - X_C)^2$$

$$\Rightarrow X_L - X_C = 0 \Rightarrow X_L = X_C$$

$$WL = \frac{1}{WC} \Rightarrow L = \frac{1}{W^2C}$$

$$L = \frac{1}{4\pi^2 f^2 C}$$

$$L = \frac{1}{4\pi^2 \times \left(\frac{360}{2\pi}\right)^2 \times 1 \times 10^{-6}}$$

$$L = 7.7H$$

$$28. \quad q_0 = CV_0 = C \times \sqrt{2} V_{rms}$$

$$q_0 = 8 \times 10^{-6} \times 220\sqrt{2} = 2.5 \times 10^{-3} C$$

$$29. \quad i = i_0 (1 - e^{-t/\tau})$$

$$\frac{di}{dt} = \frac{i_0}{\tau} e^{-t/\tau}$$

$$\text{At } t = 0, \frac{di}{dt} = \frac{i_0}{\tau}$$

$$\frac{di}{dt} = \frac{E/R}{L/R} = \frac{E}{L}$$

$$\frac{di}{dt} = \frac{200}{0.5} = 400 A/S$$

$$30. \quad \text{Area vector is in 'z' direction}$$

$$\vec{A} = L^2 \hat{k}$$

$$\phi = \vec{B} \cdot \vec{A}$$

$$= B_0 (2\hat{i} + 3\hat{j} + 4\hat{k}) \cdot L^2 \hat{k}$$

$$\phi = 4L^2 B_0 = 4B_0 L^2 \text{ wb}$$

$$31. \quad E_0 = NBAW = NBA \times 2\pi f$$

$$E_0 = 100 \times 0.05 \times 0.01 \times 2\pi \times 50 = 15.7V$$

$$I_0 = \frac{E_0}{R} = \frac{15.7}{30} = 0.524A$$

$$P_0 = E_0 I_0 = 15.7 \times 0.524$$

$$P_0 = 8.23W$$

$$32. \quad t = \frac{m \infty}{Bq}$$

$$t = \frac{1.67 \times 10^{-27}}{100 \times 10^{-3} \times 1.6 \times 10^{-19}} \times \frac{\pi}{3}$$

$$t = 1.05 \times 10^{-7} \text{ sec}$$

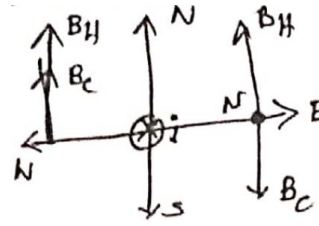
33. $\vec{a} \perp \vec{B} \Rightarrow \vec{a} \cdot \vec{B} = 0$
 $(x\hat{j} + \hat{j} - \hat{k}) \cdot (2\hat{i} + 3\hat{j} + 4\hat{k}) = 0$
 $2x + 3 - 4 = 0 \Rightarrow x = 0.5$
 $\vec{a} = 0.5\hat{i} + \hat{j} - \hat{k}$
 $a = \sqrt{0.5^2 + 1^2 + (-1)^2} = 1.5$

34. $\vec{F} = q(\vec{V} \times \vec{B})$
 $= q[(2\hat{i}) \times (\hat{i} + 2\hat{j} + 3\hat{k})]$
 $= q[4\hat{k} - 6\hat{j}]$

\vec{F} is in Y-Z Plane.

35. At 'N'

$B_c = B_H = \frac{\mu_0 i}{2\pi r}$
 $5 \times 10^{-7} = 2 \times 10^{-7} \times \frac{1}{r}$
 $r = \frac{2}{5} = 0.4m$ from the wire due east.



36. $r = \frac{i_2 R_2 - i_1 R_1}{i_1 - i_2}$
 $r = \frac{0.07 \times 20 - 0.12 \times 10}{0.12 - 0.07} = 4\Omega$
 $E = i_1 r + i_1 R_1 = i_1 (r + R_1)$
 $= 0.12(4 + 10) = 1.68V$

37. From KVL
 For ... L1
 $-5I_1 - 2I_3 + 12 = 0$ -----(1)
 $5I_1 + 2I_3 = 12$ -----(2)
 For L2
 $-3I_2 - 2I_3 + 6 = 0$
 $3I_2 + 2I_3 = 6$ -----(3)
 From 1, 2 & 3
 $I_1 = 1.549A, I_2 = 0.58A$
 $I_3 = 1.549 + 0.58 = 2.129A$

From KCL
 $I_1 + I_2 = I_3$

38. $R = \frac{rl_2}{l_1 - l_2}$
 $R = \frac{1.2 \times 500}{60} = 10\Omega$

39. $P = \frac{V^2}{R} \Rightarrow P \propto \frac{1}{R}$ but $R \propto l$
 $\Rightarrow P \propto \frac{1}{l}$

$$\Rightarrow \frac{P_1}{P_2} = \frac{l_2}{l_1} = \frac{l - \frac{10}{100}l}{l} = \frac{9}{10}$$

$$\frac{P_2 - P_1}{P_1} \times 100 = \frac{10 - 9}{9} \times 100 = 11\% \text{ Increase}$$

40. $\sigma = \frac{2\epsilon_0}{d}(V_1 - V_2) \quad \sigma = \sigma_1 - \sigma_2$

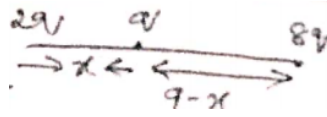
$$\sigma_1 = \frac{4Q}{A}, \quad \sigma_2 = \frac{6Q}{A}$$

$$\sigma = \sigma_1 - \sigma_2 = -\frac{2Q}{A}$$

$$\frac{2\epsilon_0}{d}(V_1 - V_2) = \frac{-2Q}{A} \Rightarrow V_1 - V_2 = \frac{-Qd}{A\epsilon_0}$$

41. $U = \frac{1}{4\pi\epsilon_0} \left[\frac{q_1q_2}{r_{12}} + \frac{q_2q_3}{r_{23}} + \frac{q_3q_1}{r_{31}} \right]$

$$U = \frac{1}{4\pi\epsilon_0} \left[\frac{2q \cdot q}{x} + \frac{q \cdot 8q}{9-x} + \frac{2q \cdot 8q}{9} \right]$$



As U is minimum $\frac{dU}{dx} = 0$

$$\frac{dU}{dx} = 2(-1)x^{-2} + 8(-1)(9-x)^{-2} - 1 = 0$$

$$\Rightarrow x = 3 \text{ cm}$$

So the charges are placed at 0, 3 and 6cm

42. $C_0 = \frac{\epsilon_0 A}{d} = 0.5$

$$C_1 = \frac{k_1 \epsilon_0 A}{d_1} = \frac{2\epsilon_0 A}{2d} = \frac{\epsilon_0 A}{d} = 0.5$$

$$C_2 = \frac{k_2 \epsilon_0 A}{d_2} = \frac{3\epsilon_0 A}{2d} = 3 \times 0.5 = 0.75$$

$$C = C_1 + C_2 = 0.5 + 0.75 = 1.25 \mu F$$

43. $E = \frac{Q}{2\pi^2 \epsilon_0 R^2} = \frac{1.4 \times 10^{-9} \times 7 \times 7}{2 \times 22 \times 22 \times 8.57 \times 10^{-12} \times \left(\frac{1}{2}\right)^2}$

$$E = 32 \text{ V/m}$$

44. $P = \sqrt{P_1^2 + P_2^2 + 2P_1P_2 \cos \theta} \quad P_1 = P_2$

$$= \sqrt{2P_1^2 + 2P_1^2 \cos 60^\circ}$$

$$= \sqrt{3}P_1 = \sqrt{3} \times q \times l$$

$$\vec{P} = -\sqrt{3} q l \hat{j}$$

45. $s = ut + \frac{1}{2}at^2, \quad a = \frac{qE}{m}$

$$a = \frac{1.6 \times 10^{-19} \times 2 \times 10^4}{9 \times 10^{-31}} = \frac{32}{9} \times 10^{15}$$

$$1.5 \times 10^{-2} = \cos t + \frac{1}{2} \times \frac{32}{9} \times 10^{15} t^2$$

$$t = \sqrt{\frac{135}{16}} \times 10^{-9} = 2.9 \times 10^{-9} \text{ sec.}$$

Numerical Value Questions:-

46. $T = 2\pi \sqrt{\frac{L}{g}} = \frac{45}{20}, a = \frac{qE}{m}$

$$T^1 = 2\pi \sqrt{\frac{L}{g-a}} = 2\pi \sqrt{\frac{L}{g - \frac{qE}{m}}}$$

$$\frac{T}{T^1} = \sqrt{\frac{g - \frac{qE}{m}}{g}} = \sqrt{1 - \frac{qE}{mg}}$$

$$\frac{T}{T^1} = \sqrt{1 - \frac{4 \times 10^{-6} \times 2.5 \times 10^4}{40 \times 10^{-3} \times 10}}$$

$$\frac{45}{20 \times T^1} = \sqrt{1 - 0.25}$$

$$T^1 = 2.6 \text{ sec}$$

$$t = T^1 \times 20 = 2.6 \times 20 = 52 \text{ sec.}$$

47. $V_{(1,2,3)} - V_{(0,0,0)} = \int_{(0,0,0)}^{(1,2,3)} \vec{E} \cdot d\vec{r}$

$$= - \left[\int_0^1 E_x dx + \int_0^2 E_y dy + \int_0^3 E_z dz \right]$$

$$= - \left[\int_0^1 10x dx + \int_0^2 30y dy + \int_0^3 40z dz \right]$$

$$= - \left[\frac{10}{2} (x^2)_0^1 + \frac{30}{2} (y^2)_0^2 + \frac{40}{2} (z^2)_0^3 \right]$$

$$= - \left[5(1^2 - 0) + 15(2^2 - 0) + 20(3^2 - 0) \right]$$

$$= - [5 + 60 + 180] = -245V$$

48. For first balance point

$$\frac{R}{S} = \frac{l}{100-l} = \frac{33.7}{66.3}$$

$$\text{Second time } S^1 = \frac{12S}{12+S}$$

For second balance point

$$\frac{R}{S^1} = \frac{l^1}{100-l^1} = \frac{51.9}{48.1}$$

$$\frac{R}{\frac{12S}{12+S}} = \frac{51.9}{48.1}$$

$$= \frac{51.9}{48.1} = \frac{S+12}{12} \times \frac{33.7}{66.3}$$

$$S = 13.47 \Omega$$

$$49. \quad \vec{V} // \vec{B} \Rightarrow \frac{V_x}{B_x} = \frac{V_y}{B_y} = \frac{V_z}{B_z}$$

$$\frac{4}{3} = \frac{-x}{6} = \frac{y}{6}$$

$$\frac{4}{3} = \frac{-x}{6} \Rightarrow x = -8$$

$$\frac{4}{3} = \frac{y}{6} \Rightarrow y = 8$$

$$\vec{V} = 4\hat{i} + 8\hat{j} + 8\hat{k}$$

$$V = \sqrt{4^2 + 8^2 + 8^2} = 12 \text{ ms}^{-1}$$

$$50. \quad E = \frac{d\phi}{dt} = \frac{d}{dt}(5t^3 + 4t^2 + 2t - 5)$$

$$E = 15t^2 + 8t + 2$$

$$\text{at } t = 2 \text{ sec}$$

$$E = 15(2^2) + 8(2) + 2 = 78 \text{ V}$$

$$i = \frac{E}{R} = \frac{78}{5} = 15.6 \text{ A}$$

CHEMISTRY

51. $-OCH_3$ group is +ME group which activates the benzene ring.

52. Alkene with large ring size exhibit geometrical Isomerism

53. C,D are Non-planar molecules

54. Conceptual

55. Conceptual

56. Conceptual

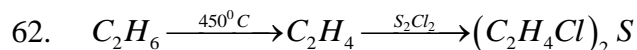
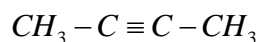
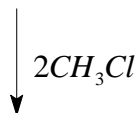
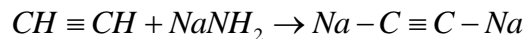
57. The reactivity of Bromination : $3^0 > 2^0 > 1^0$.

58. According to $4\pi\epsilon_s$.

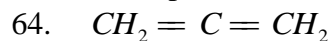
59. Conceptual

60. Conceptual

61.



63. Conceptual



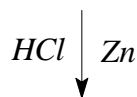
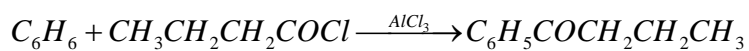
65. Conceptual

66. Conceptual

67. Conceptual

68. Conceptual

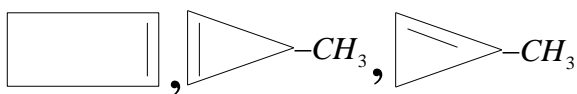
69.



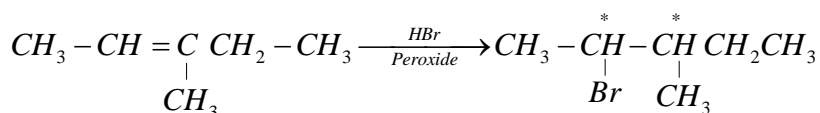
70. Conceptual

Numerical Value Questions:-

71.



72.



2-Chiral centres,

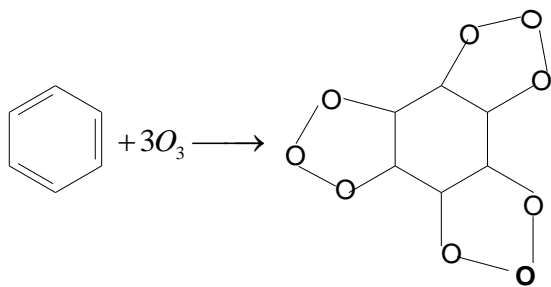
 No. of stereo Isomers = $2^2 = 4$

73.

$$\%N = \frac{1.4 \times N \times V(m_1)}{W}$$

$$= \frac{1.4 \times 0.1 \times 5}{0.0295} = 23.7$$

74.



75. 1-Butene, cis and trans -2-butene, 2-methyl propene