



# SRIGAYATRI EDUCATIONAL INSTITUTIONS INDIA

SR MPC  
Time: 3 Hours

**JEE MAINS - GT 5**

Date: 09-07-2020  
Max Marks : 300

## KEY SHEET

### MATHS

1) <b>B</b>	2) <b>A</b>	3) <b>C</b>	4) <b>A</b>	5) <b>A</b>	6) <b>B</b>	7) <b>C</b>	8) <b>B</b>	9) <b>B</b>	10) <b>C</b>
11) <b>A</b>	12) <b>B</b>	13) <b>D</b>	14) <b>A</b>	15) <b>D</b>	16) <b>C</b>	17) <b>C</b>	18) <b>B</b>	19) <b>C</b>	20) <b>A</b>
21) <b>-3</b>	22) <b>11</b>	23) <b>2</b>	24) <b>5</b>	25) <b>28</b>					

### PHYSICS

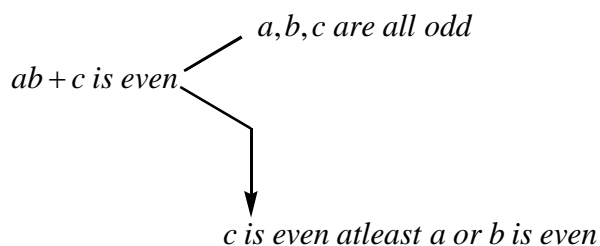
26) <b>C</b>	27) <b>D</b>	28) <b>A</b>	29) <b>D</b>	30) <b>A</b>	31) <b>A</b>	32) <b>A</b>	33) <b>B</b>	34) <b>C</b>	35) <b>C</b>
36) <b>B</b>	37) <b>A</b>	38) <b>B</b>	39) <b>D</b>	40) <b>D</b>	41) <b>B</b>	42) <b>C</b>	43) <b>D</b>	44) <b>D</b>	45) <b>C</b>
46) <b>250</b>	47) <b>200</b>	48) <b>2.5</b>	49) <b>3.2</b>	50) <b>150</b>					

### CHEMISTRY

51) <b>A</b>	52) <b>D</b>	53) <b>D</b>	54) <b>B</b>	55) <b>A</b>	56) <b>B</b>	57) <b>A</b>	58) <b>A</b>	59) <b>D</b>	60) <b>D</b>
61) <b>A</b>	62) <b>D</b>	63) <b>D</b>	64) <b>C</b>	65) <b>A</b>	66) <b>D</b>	67) <b>B</b>	68) <b>D</b>	69) <b>B</b>	70) <b>D</b>
71) <b>4</b>	72) <b>8</b>	73) <b>75</b>	74) <b>0.05</b>	75) <b>-96</b>					

## HINTS & SOLUTIONS MATHEMATICS

01.  $P(\text{number chosen is odd}) = 3/5$   
 $P(\text{number chosen is even}) = 2/5$



E:  $(ab + c)$  is even note that even  $E$  can occurs in two cases

$E_1$  : all the three numbers a, b and 'c' are odd  $P(E_1) = \left(\frac{3}{5}\right)^3 = \frac{27}{125}$

$E_2$  : 'c' is even and at least one of a or b is even  $P(E_2) = \frac{2}{5} \left(1 - \frac{9}{25}\right) = \frac{2}{5} \cdot \frac{16}{25} = \frac{32}{125}$

$P(E) = P(E_1 \text{ or } E_2)$

$$= P(E_1) + P(E_2)$$

$$= \frac{59}{125}$$

02.

Let  $g(x) = (\sin x)^{\ln x} = e^{\ln x \cdot \ln(\sin x)}$

$$f(x) = g'(x) = (\sin x)^{\ln x} \left[ \cot x (\ln x) + \frac{\ln(\sin x)}{x} \right]$$

Hence  $f\left(\frac{\pi}{2}\right) = g'\left(\frac{\pi}{2}\right) = 1(0+0) = 0$

03.  $f''(x)$  is an odd function

$$\therefore \phi \alpha, \beta = 0 \Rightarrow \sin^4 \alpha - 1^2 + \cos^4 \beta - 1^2 + 2 \sin^2 \alpha - \cos^2 \beta^2 = 0$$

$$\Rightarrow \sin^2 \alpha + \sin^2 \beta = 1$$

04. The given equation denotes that PA+PB=13  
Point P lies on line segment AB

05.  $y = x^{3/2}; \frac{dr}{dt} = 11$

$$\frac{dx}{dt} \text{ when } x = 3$$

$$r^2 = x^2 + y^2 \Rightarrow r = 6$$

$$r \frac{dr}{dt} = x \frac{dx}{dt} + y \frac{dy}{dt} \dots\dots\dots(1)$$

Also,  $\frac{dy}{dt} = \frac{3}{2} \sqrt{x} \frac{dx}{dt} \dots\dots(2)$

$$r \frac{dr}{dt} = x \frac{dx}{dt} + y \frac{3}{2} \sqrt{x} \frac{dx}{dt}$$

$$r \frac{dr}{dt} = \left( x + \frac{3y\sqrt{x}}{2} \right) \frac{dx}{dt}$$

$$6 \cdot 11 = \left( 3 + \frac{3 \cdot 3 \cdot \sqrt{3} \cdot \sqrt{3}}{2} \right) \frac{dx}{dt}$$

$$66 = \left( 3 + \frac{27}{2} \right) \frac{dx}{dt}$$

$$\Rightarrow 66 = \left( \frac{33}{2} \right) \frac{dx}{dt}$$

$$\Rightarrow \frac{dx}{dt} = 4$$

06. D.R's normal to the plane P1 is parallel to  $(2j + 3k) \times (4j - 3k)$

$$\begin{vmatrix} i & j & k \\ 0 & 2 & 3 \\ 0 & 4 & -3 \end{vmatrix}$$

$$i(-6 - 12) = -18i$$

D.R's normal to the plane P2 is parallel to  $(j - k) \times (3i + 3j)$

$$\begin{vmatrix} i & j & k \\ 0 & 1 & -1 \\ 3 & 3 & 0 \end{vmatrix}$$

$$i(3) - j(3) + k(-3)$$

D.R's parallel to the line of intersection of planes  $P_1$  and  $P_2$  is

$$\begin{vmatrix} i & j & k \\ -1 & 0 & 0 \\ 1 & -1 & -1 \end{vmatrix} = i(0) - j(1) + k(1) = -j + k$$

$$= (0, -1, 1)$$

$$\text{Angle between } \cos \theta = \frac{|0-1-2|}{3\sqrt{2}}$$

$$\theta = \frac{\pi}{4}$$

$$07. (\sin x + \cos x) + \left(\frac{\sin x}{\cos x} + \frac{\cos x}{\sin x}\right) + \left(\frac{1}{\cos x} + \frac{1}{\sin x}\right) = 7$$

$$(\sin x + \cos x) + \frac{1}{\sin x \cos x} + \left(\frac{\sin x + \cos x}{\sin x \cos x}\right) = 7$$

$$(\sin x + \cos x) \left(1 + \frac{2}{\sin 2x}\right) = 7 - \frac{2}{\sin 2x}$$

Squaring we get

$$(1 + \sin 2x) \left(1 + \frac{4}{\sin^2 2x} + \frac{4}{\sin 2x}\right) = 49 + \frac{4}{\sin^2 2x} - \frac{28}{\sin 2x}$$

$$\Rightarrow \sin^3 2x - 44 \sin^2 2x + 36 \sin 2x = 0$$

$$\sin^2 2x - 44 \sin 2x + 36 = 0 \quad \because \sin 2x \neq 0$$

$$\therefore \sin 2x = 22 - 8\sqrt{7} \therefore a = 22 \quad b = 8$$

$$08. \sin \cos^{-1}(\cos(\tan^{-1} x)) = p$$

$$\text{For } x \in R; \tan^{-1} x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$$

$$\cos(\tan^{-1} x) \in (0, 1]$$

$$\cos^{-1} \cos(\tan^{-1} x) \in \left[0, \frac{\pi}{2}\right)$$

$$\sin[\cos^{-1} \cos(\tan^{-1} x)] \in [0, 1)$$

$$09. \text{Equation of pair of tangents, } (a^2 - 1)y^2 - x^2 + 2ax - 1 = 0$$

$$\text{angle between them, } \tan \theta = \frac{2\sqrt{h^2 - ab}}{a+b} = \frac{2\sqrt{a^2 - 1}}{a^2 - 2} < 0 \Rightarrow a \in (-\sqrt{2}, -1) \cup (1, \sqrt{2})$$

10.

P	q	$p \rightarrow q$	$\sim p$	$\sim pvq$	$p \rightarrow q \leftrightarrow (\sim pvq)$
T	T	T	F	T	T
T	F	F	F	F	T
F	T	T	T	T	T
F	F	T	T	T	T

$$11. x_1 + x_2 = 15; x_r \geq 0; r = 2, n = 15$$

No. of non negative integral solutions  $= {}^{n+r-1}C_{r-1} = {}^{16}C_1 = 16$

$$x_1 + x_2 + x_3 + x_4 + x_5 = 20$$

$$x_3 + x_4 + x_5 = 5 \Rightarrow {}^{5+3-1}C_{3-1} = {}^7C_2 = 21$$

Total no. of solutions =  $16 \times 21 = 336$

$$12. \quad \bar{x} = \frac{1.1^2 + 2.2^2 + 3.3^2 + \dots + n.n^2}{1^2 + 2^2 + \dots + n^2} = \frac{\sum n^3}{\sum n^2} = \frac{3n(n+1)}{2(2n+1)}$$

$$13. \quad \text{put } \sqrt{x-1} = t \text{ or } x = t^2 + 1$$

$$\sqrt{t^2 + 4 - 4t} + \sqrt{t^2 + 9 - 6t} = 1$$

$$\Rightarrow \sqrt{(t-2)^2} + \sqrt{(t-3)^2} = 1 \Rightarrow |t-2| + |t-3| = 1$$

This equation is satisfied for all values of t between 2 and 3 that is  $2 \leq t \leq 3$  thus the given equation satisfied for all values of x lying between 5 and 10

$$14. \quad f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{f\left(\frac{2x+2h}{2}\right) - f(x)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{f(2x) + f(2h) - f(x)}{2h}$$

$$\text{We have } f\left(\frac{x+y}{2}\right) = \frac{f(x) + f(y)}{2}$$

$$x = 2x, y = 0 \text{ then } f(x) = \frac{f(2x) + f(0)}{2}$$

$$f(2x) = 2f(x) - f(0)$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{2f(x) - f(0) + 2f(h) - f(0) - 2f(x)}{2h}$$

$$\lim_{h \rightarrow 0} \frac{f(h) - f(0)}{h} = f'(0) = -1$$

$$15. \quad 2^{n\left(\frac{n+1}{2}\right)} = 2^{7 \times 4} = 2^{28}$$

16. Let  $\alpha, \beta$  be roots and

$$\alpha > 2 \quad \beta < 2$$

$$(\alpha - 2)(\beta - 2) < 0$$

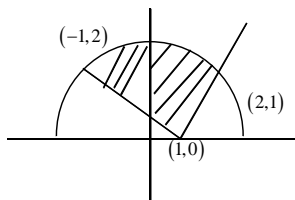
$$\alpha\beta - 2(\alpha + \beta) + 4 < 0$$

$$k^2 + k - 8 - 2(k+1) + 4 < 0$$

$$k^2 - k - 6 < 0$$

$$(k-3)(k+2) < 0, \text{ also } \Delta > 0 \Rightarrow 3k^2 + 2k - 33 < 0 \Rightarrow (3k+11)(k-3) < 0 \Rightarrow \frac{-11}{3} < k < 3,$$

$$-2 < k < 3$$

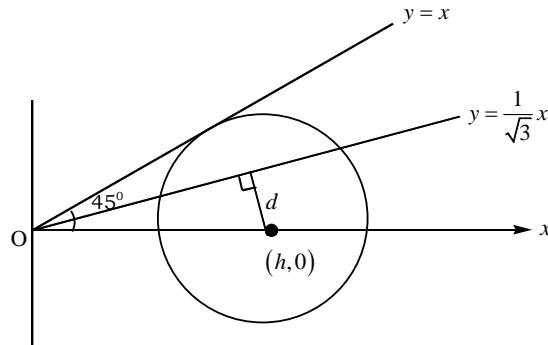


17.

$$\begin{aligned} \text{Area} &= \int_{-1}^2 (\sqrt{5-x^2} - |x-1|) dx \\ &= \int_{-1}^2 \sqrt{5-x^2} dx + \int_{-1}^1 (x-1) dx - \int_1^2 (x-1) dx \end{aligned}$$

18.

$$\begin{aligned} r &= \frac{h}{\sqrt{2}} \text{ and } d = \frac{h}{2} \\ 2\sqrt{\frac{h^2}{2} - \frac{h^2}{4}} &= 2 \Rightarrow h = 2 \\ r &= \sqrt{2} \end{aligned}$$



19. 
$$f(x) = \begin{cases} -2x & \text{for } x \leq -1 \\ 2 & \text{for } -1 \leq x \leq 1 \\ 2x & \text{for } x \geq 1 \end{cases}$$

F is diff in  $(-1,1)$

20. Let the line be  $\frac{x}{a} = \frac{y}{b} = \frac{z}{c}$

This intersects the given line

$$\begin{vmatrix} 1 & -3 & 5 \\ a & b & c \\ 2 & 4 & 3 \end{vmatrix} = 0 \text{ and } \begin{vmatrix} 4 & -3 & 14 \\ a & b & c \\ 2 & 3 & 4 \end{vmatrix} = 0$$

21. Slope of the give line =  $-\frac{3}{2}$

The points on the curve at which the tangent is parallel to the given line. So, differentiating both sides with respect to x of  $3x^2 - 4y^2 = 72$  we get

$$\frac{dy}{dx} = \frac{3x}{4y} = \frac{-3}{2} \text{ (given)}$$

$$\Rightarrow \frac{x}{y} = -2$$

$$\text{Now } 3\left(\frac{x}{y}\right)^2 - 4 = \frac{72}{y^2} \Rightarrow y^2 = 9 \Rightarrow y = -3, 3$$

So, points are  $(-6, 3)$  and  $(6, -3)$

$$\text{Now, distance of } (-6, 3) \text{ from the given line} = \left| \frac{-18+6+1}{\sqrt{13}} \right| = \frac{11}{\sqrt{13}}$$

$$\text{And distance of } (6, -3) \text{ from the given line} = \left| \frac{18-6+1}{\sqrt{13}} \right| = \frac{13}{\sqrt{13}}$$

Clearly, the required point is on  $(-6, 3) = (x_o, y_o)$  (given)

$$\text{So, } x_o = -6, y_o = 3$$

$$\text{Hence } (x_o + y_o) = -6 + 3 = -3$$

22.

$$|P| = 1(12 - 12) - \alpha(4 - 6) + 3(4 - 6)$$

$$= 2\alpha - 6$$

$$|P| = |A|^2 = 16$$

$$2\alpha - 6 = 16$$

$$\alpha = 11.$$

23.  $k = 2,$

Let  $e^{i\frac{2\pi}{n}} = \alpha$  then  $\sum_{j=1}^{n-1} \frac{1}{1-e^j} = \frac{1}{1-\alpha} + \frac{1}{1-\alpha^2} + \dots + \frac{1}{1-\alpha^{n-1}}$

Where  $\alpha$  is a  $n$ th root of unity ( $\alpha, \alpha^2, \alpha^3, \dots, \alpha^{n-1}$ ) are the roots of

$$\frac{x^n - 1}{x - 1} = (x - \alpha)(x - \alpha^2) \dots (x - \alpha^{n-1})$$

Taking log on both side

$$\log \frac{x^n - 1}{x - 1} = \log(x - \alpha) + \log(x - \alpha^2) + \dots + \log(x - \alpha^{n-1})$$

Diff w.r.t.  $x$  and use  $\lim_{x \rightarrow 1}$

$$\Rightarrow \frac{n-1}{2} = \frac{1}{1-\alpha} + \frac{1}{1-\alpha^2} + \dots + \frac{1}{1-\alpha^{n-1}}$$

24.

$$\int_{-2}^2 f(x) dx = \int_{-2}^0 (x - [x]) dx + \int_0^2 (x + |x|) dx = 5$$

25.

The coefficient of  $x^6$  in the given expression = coefficient of  $x^6$  in  $(1 + {}^6C_1x^6)(1 + {}^5C_1x^5)(1 + {}^4C_1x^4)(1 + {}^3C_1x^3 + {}^3C_2x^6)(1 + {}^2C_1x^2 + {}^2C_2x^4)(1 + x)$

= coefficient of  $x^6$  in  $(1 + 6x^6 + 5x^5 + 4x^4)(1 + 2x^2 + 3x^3 + x^4 + 6x^5 + 3x^6)(1 + x)$

= coefficient of  $x^6$  in  $(11x^5 + 17x^6)(1 + x)$

= 28

### PHYSICS

26.

$$T = 2\pi\sqrt{\frac{l}{g}} \text{ or } g = 4\pi^2 \frac{l}{T^2}$$

or  $\log g = \log(4\pi^2) + \log l - 2 \log T$ . The maximum error in  $g$  is

$$\frac{\Delta g}{g} = \frac{\Delta l}{l} + 2 \frac{\Delta T}{T} = 2\% + 2 \times 3\% = 8\%$$

27.

Refer to Fig. A is the highest point on the trajectory

$$\text{Average velocity} = \frac{\text{displacement } OA}{\text{time taken}}$$

$$= \frac{\sqrt{h_{\max}^2 + \frac{R^2}{4}}}{\frac{1}{2}t_f}$$

Where  $h_{\max} = \frac{u^2 \sin^2 \theta}{2g}$

$$R = \frac{u^2 \sin^2 2\theta}{g}$$

$$\text{and } t_f = \frac{2u \sin \theta}{g}$$

Using these in Eq. (1) and simplifying we get average velocity =  $\frac{u}{2}(1 + 3\cos^2 \theta)^{1/2}$

So the correct choice is (d)

28. The forces acting on the balloon are its weight acting downwards and upthrust F acting upwards.  
Thus

$$F - Mg = Ma$$

When mass m is removed, we have

$$F - (M - m)g = (M - m)a'$$

Where a' is the new acceleration. Eliminating F from (i) and (ii) and simplifying we get

$$a' = \frac{Ma + mg}{M - m}$$

Which is choice

29. The velocity attained after a fall through a height h is given by

$$v^2 = 2gh$$

Thus  $h \propto v^2$ . The velocity after first rebound is  $ev$ . Therefore, the height attained after first rebound =  $e^2h$ . Velocity after second rebound is  $e^2v$ . Hence the height attained after second rebound is  $e^4h$ . Thus the correct choice is

30. From the law of conservation of angular momentum we have

$$I\omega = I'\omega'$$

Here  $I = MR^2$  and  $I' = (M + 2m)R^2$ . Therefore

$$\frac{\omega'}{\omega} = \frac{I}{I'} = \frac{M}{(M + 2m)}$$

Hence the correct choice

32. Using Bernoulli's theorem, we have

$$\frac{1}{2}\rho v^2 = p = \rho gh$$

$$\text{or } h = \frac{v^2}{2g}$$

Now  $v = r\omega = r(2\pi v)$ . Using this in (1) we get

$$h = \frac{2\pi^2 v^2 r^2}{g}$$

Given  $v = 2 \text{ rev. per second}$ ,  $r = 0.05 \text{ m}$ ,  $g = 10 \text{ ms}^{-2}$  and  $\pi^2 = 10$

Using these values, we get  $h = 0.02 \text{ m} = 2 \text{ cm}$ , which is choice

33. Let  $\theta_1$  and  $\theta_2$  be the temperatures at the two faces of the composite slab and let  $\theta$  be the temperature at the common face of the slab. If  $l$  is the length of each slab and A the area of their face, then in the steady state, the rate of flow of heat across A = rate of flow of heat across B, ie

$$\frac{k_1 A (\theta_1 - \theta)}{l} = \frac{k_2 A (\theta - \theta_2)}{l}$$

$$\text{or } k_1 (\theta_1 - \theta) = k_2 (\theta - \theta_2)$$

Now  $k_2 = 2k_1$ . Therefore

$$(\theta_1 - \theta) = 2(\theta - \theta_2)$$

Also,  $\theta_1 - \theta_2 = 12^\circ \text{C}$  or  $\theta_2 - \theta_1 = -12$

Using (ii) in (i) we have

$$(\theta_1 - \theta) = 2\{\theta - (\theta_1 - 12)\}$$

$$\text{or } 3(\theta_1 - \theta) = 24$$

$$\text{or } \theta_1 - \theta = 8^\circ \text{C}$$

Hence the correct choice

34. The velocity of transverse waves is given by  $v = \sqrt{T/m}$  where  $T$  = tension and  $m$  = mass per unit length of the wire. If  $r$  is the radius of the wire and  $\rho$  its density, then  $m = \pi r^2 \rho$ . Therefore,

$$v = \frac{\sqrt{T}}{r\sqrt{\pi\rho}}. \text{ Thus } v_A = \frac{\sqrt{T_A}}{r_A\sqrt{\pi\rho}}$$

$$\text{and } v_B = \frac{\sqrt{T_B}}{r_B\sqrt{\pi\rho}}$$

$$\text{Now } \frac{v_A}{v_B} = \sqrt{\frac{T_A}{T_B} \cdot \frac{r_B}{r_A}}$$

It is given that  $r_A = 2 r_B$  and  $T_A = \frac{1}{2} T_B$ . Hence

$$\frac{v_A}{v_B} = \frac{1}{2\sqrt{2}}. \text{ The correct choice is}$$

35. Given  $I = 1 \text{mA} = 10^{-3} \text{A}$ ,  $G = 20 \Omega$  and  $R = 4980 \Omega$

$$\text{Now } I = \frac{V}{R+G}$$

$$\text{or } V = I(R+G) = 10^{-3} \times (4980 + 20) = 5.0 \text{V}$$

Hence the correct choice is

36. Given  $v = (3\hat{i} + 2\hat{j}) \text{ms}^{-1}$  and  $B = (2\hat{j} + 3\hat{k})$  tesla.

Force experienced by the proton is

$$F = q(v \times B) = q(3\hat{i} + 2\hat{j}) \times (2\hat{j} + 3\hat{k})$$

$$= q(6\hat{i} \times \hat{j} + 9\hat{i} \times \hat{k} + 4\hat{j} \times \hat{j} + 6\hat{j} \times \hat{k})$$

$$= q(6\hat{k} - 9\hat{j} + 0 + 6\hat{i})$$

$$= 3q(2\hat{i} - 3\hat{j} + 2\hat{k}) \text{ newton}$$

$$\therefore \text{Acceleration} = \frac{F}{m} = \frac{3q}{m}(2\hat{i} - 3\hat{j} + 2\hat{k})$$

$$= 3 \times (0.96 \times 10^8)(2\hat{i} - 3\hat{j} + 2\hat{k})$$

$$= 2.88 \times 10^8 (2\hat{i} - 3\hat{j} + 2\hat{k}) \text{ms}^{-2}$$

Hence the correct choice is

37. Let  $I_0$  be the maximum current and  $I$  be the current at time  $t$  when the energy stored in inductor becomes  $1/9$  of the maximum energy, then

$$\frac{1}{2} LI^2 = \frac{1}{9} \times \frac{1}{2} LI_0^2 \Rightarrow I = \frac{I_0}{3} \Rightarrow I_0 = 3I$$

$$\text{Time constant } \tau = \frac{L}{R} = \frac{100 \times 10^{-3}}{0.2} = \frac{1}{2} \text{ second}$$

$$\text{Now } I = I_0(1 - e^{-t/\tau})$$

$$\Rightarrow I = 3I(1 - e^{-t/\tau})$$



$$\Rightarrow e^{-t/\tau} = \frac{2}{3}$$

$$\Rightarrow e^{t/\tau} = \frac{3}{2}$$

$$\Rightarrow \frac{t}{\tau} = \ln\left(\frac{3}{2}\right)$$

$$t = \tau \ln\left(\frac{3}{2}\right) = \frac{1}{2} \ln\left(\frac{3}{2}\right) \text{ second}$$

So the correct choice is

38. Impedance  $z = \sqrt{R^2 + (\omega L)^2}$  and  $I_0 = \frac{V_0}{Z}$ . As  $\omega$  is increased,  $Z$  increase. Hence current  $I_0$  decreases. As a result the brightness of the bulb will decrease. So the correct choice is

39.  $B_0 = \frac{E_0}{c} = \frac{6.0 \times 10^{-4}}{3 \times 10^8} = 2.0 \times 10^{-12} T$  which is choice is

40.  $E = \frac{1}{2}mv^2 = h\nu_0 - W_0$ . Now  $E_1 = 2 - 1 = 1eV$  and

$E_2 = 10 - 1 = 9eV$ . Therefore  $E_1 / E_2 = 1/9$  i.e

$$\frac{\frac{1}{2}mv_1^2}{\frac{1}{2}mv_2^2} = \frac{1}{9}$$

or  $\frac{v_1}{v_2} = \frac{1}{3}$ . Hence the correct choice is

41. The longest wavelengths in the two series are given by

$$\frac{1}{\lambda_L} = R \left( \frac{1}{1^2} - \frac{1}{2^2} \right) = R \cdot \frac{3}{4}$$

and  $\frac{1}{\lambda_B} = R \left( \frac{1}{2^2} - \frac{1}{3^2} \right) = R \cdot \frac{5}{36}$

$$\therefore \frac{\lambda_B}{\lambda_L} = \frac{3}{4} \times \frac{36}{5} = \frac{27}{5} \text{ or } \lambda_L : \lambda_B = 5 : 27$$

42. A pn junction diode is formed by joining a p-type semiconductor to an n-type semiconductor. Separately, the two semiconductors are electrically neutral. When they are joined, some electrons near the junction diffuse from the n-type into the p-type semiconductor, where they fill a few of the holes. Consequently, the n-type is left with a positive charge and the p-type acquires a net negative charge. Therefore a potential difference is established, with the n-type at a higher potential than the p-type. Hence an electric field is set up at the junction and it is directed from the n-type side to the p-type side. Thus the correct choice is

43. Gate P is OR gate and gate Q is AND gate. The output of gate Q is  $X = 1$  only if  $D=1$  and  $C=1$  If  $A=1$  and  $B=1$  then  $D=1$ . So the only correct choice is

44.  $\lambda_{\min} = \frac{\lambda}{4}$

45.  $F = 6\pi\eta r v$

$$F' = 6\pi\eta \left( \frac{r}{2} \right) \times \left( \frac{v}{2} \right) = \frac{1}{4} \times 6\pi\eta r v = \frac{F}{4}$$

So the correct choice is

46. sol: As  $\frac{P_2}{P_1} = \frac{T_2}{T_1}$ ,  $\frac{\left(P + \frac{0.4}{100}P\right)}{P} = \frac{T+1}{T}$

or  $1 + \frac{0.4}{100} = 1 + \frac{1}{T}$

Whence,  $T = 250 K$

47.  $T_1 = 127^\circ C = 127 + 273 = 400 K$ ,  $T_2 = 27^\circ C = 300 K$ ,  $Q = 800 J$

The efficiency of the engine is given by

$$\eta = \frac{W}{Q} = 1 - \frac{T_2}{T_1}$$

$$\therefore \text{Work done } W = Q \left(1 - \frac{T_2}{T_1}\right)$$

$$= 800 \times \left(1 - \frac{300}{400}\right) = 200 J$$

Hence the correct choice is

48. Potential difference between the plates before the slab is introduced is

$$V = E \times d = 200 \times 0.05 = 10V$$

The capacitance of the capacitor is given by

$$C = \frac{\epsilon_0 A}{d} = \frac{\epsilon_0 A}{0.05} \text{ or } \epsilon_0 A = 0.05 C$$

When a slab of dielectric constant K and thickness t is introduced, the capacitance becomes

$$C' = \frac{\epsilon_0 A}{d - t \left(1 - \frac{1}{K}\right)} = \frac{0.05 C}{0.05 - 0.01 \left(1 - \frac{1}{4}\right)} = \frac{20C}{17}$$

Now  $Q = CV = C'V'$ . Therefore

$$V' = \frac{CV}{C'} = \frac{CV}{20C/17} = \frac{17V}{20} = \frac{17 \times 10}{20} = 8.5V$$

49. Given  $\beta = 4.0 mm$  and  $\lambda = 6000 \text{ \AA}$

We know that the fringe width is given by

$$\beta = \frac{\lambda D}{d}$$

for  $\lambda' = 4800 \text{ \AA}$ , the fringe width will be

$$\beta' = \frac{\lambda' D}{d}$$

From (i) and (ii) we have

$$\beta' = \beta \frac{\lambda'}{\lambda} = \frac{4.0 mm \times 4800 \text{ \AA}}{6000 \text{ \AA}} = 3.2 mm$$

50. Friction force  $= \mu mg = 0.2 \times 5 \times 10 = 10 N$ . Effective force  $F = \text{applied force} - \text{frictional force} = 25 - 10 = 15 N$ . Kinetic energy = work done by force F in pulling the body through a distance  $S (= 10 m) = 15 \times 10 = 150 J$ , which is choice is

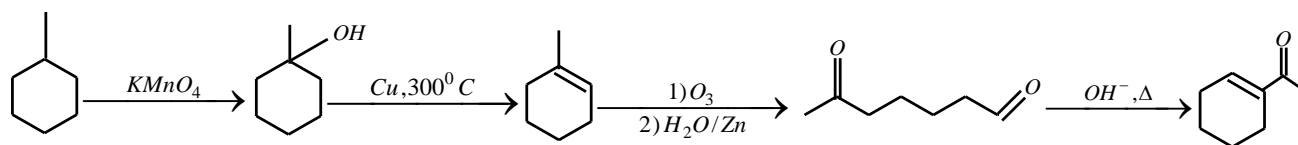
### CHEMISTRY

51. NCERT – XI, VOL – II, P.NO: 277, 278, 281, 287

52. NCERT – XI, VOL – II, P.NO: 313

53. NCERT – XII, VOL – I, P.NO: 220

54. NCERT – XII, VOL – I, P.NO:199  
 55. NCERT – XI, VOL – I, P.NO: 127  
 57. NCERT – XI, VOL – II, P.NO: 407  
 58.



60. NCERT – XII, VOL – II, P.NO: 291  
 61. NCERT – XI, VOL – I, P.NO: 183  
 $\Delta = -10 \times 75.3 - 6030 - 36.8 \times 10$   
 $= -753 - 6030 - 368 = -7151 J$   
 62. NCERT – XI, VOL – I, P.NO: 36  
 63. NCERT – XII, VOL – II, P.NO: 399  
 64. NCERT – XI, VOL – II, P.NO: 350  
 68. NCERT – XI, VOL – I, P.NO: 228, Q.NO: 7.45

$[H^+]$  from  $H_2S$  is negligible when compared with,  $[H^+]$  from  $HCl$

$$K_{a1} = \frac{[H^+][HS^-]}{[H_2S]} \Rightarrow [HS^-] = K_{a1} \frac{[H_2S]}{[H^+]} = 9.1 \times 10^{-8} \times \frac{10^{-1}}{10^{-3}}$$

$$= 9.1 \times 10^{-6} M$$

$$K_{a1} K_{a2} = \frac{[H^+]^2 [S^{2-}]}{[H_2S]} [S^{2-}] = \frac{9.1 \times 10^{-8} \times 1.2 \times 10^{-13} \times 0.1}{(10^{-3})^2}$$

$$= 10.92 \times 10^{-16} M$$

69. NCERT – XII, VOL – I, P.NO: 62

$$P_{\text{Benzene}} = \frac{1}{5} \times 50 = 10 \text{ mm of Hg}$$

$$P_{\text{Toluene}} = \frac{4}{5} \times 30 = 24 \text{ mm of Hg}$$

$$\text{In vapour phase } x_{\text{Benzene}} = \frac{10}{34} = 0.29$$

70. NCERT – XII, PART – I, P.NO: 130  
 71. NCERT – XI, VOL – I, P.NO: 265  
 73. NCERT – XI, VOL – II, P.NO: 358

$$\omega\% \text{ of } N = \frac{1.4 \times 10 \times 2}{0.5} = 56\%$$

$$56 = \frac{14 \times 3}{G.M.W(\text{ing})} \times 100 \Rightarrow G.M.W = 75 g$$

74. NCERT – XII, VOL – I, P.NO: 98

$$\text{Average rate} = \frac{1}{2} \left[ -\frac{\Delta[A]}{\Delta t} \right] = \frac{1}{2} \times \frac{6}{60} = 0.05 \text{ mole } |lt| \text{ min}$$

75.  $E_{MnO_4^-/Mn^{2+}} = E_{MnO_4^-/Mn^{2+}}^0 - \frac{0.06}{5} \log \frac{[Mn^{2+}]}{[MnO_4^-][H^+]^8}$
- $$= E_{MnO_4^-/Mn^{2+}}^0 - 0.012 \log \frac{[Mn^{2+}]}{[MnO_4^-]} - 0.096 pH$$