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**SRIGAYATRI EDUCATIONAL INSTITUTIONS**  
**INDIA**

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**MOTION IN STRAIGHT LINE UT-04 QB****PHYSICS**

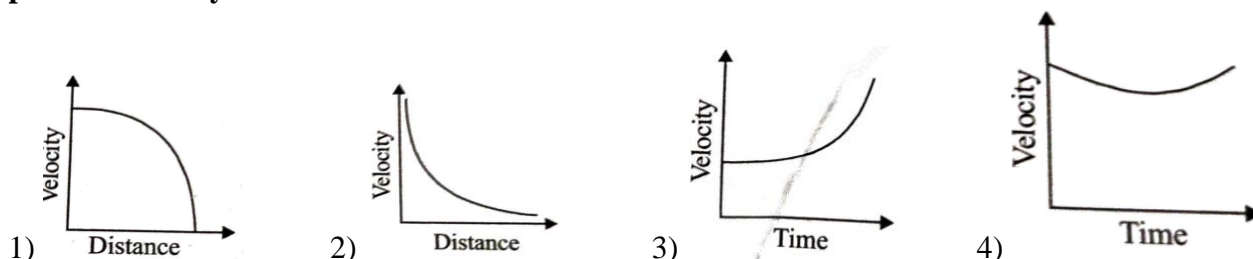
1. A car moving along a straight highway with speed of  $252\text{kmh}^{-1}$  is brought to a stop with in a distance of 400m. What is the retardation of the car (assumed uniform). How long does it take for the car to stop ....
2. Two trains A & B of length 400m each are moving on two parallel takes with a uniform speed 72 km/h in the same direction, with A a head of B. The driver of B decides to overtake A and accelerates by  $1\text{ms}^{-2}$ . If after 50s, the guard of B just move past the diver of A. What was the original distance between them ?
3. A jet airplane travelling at the speed of  $1500\text{kmh}^{-1}$  ejects the products of combustion at the speed of  $2500\text{kmh}^{-1}$  relative to the jet plane. What is the speed of the latter with respect to an observer on the ground? (km/h)
4. The position of an object moving along x -axis is given by  $x=p+Qt^2$  where  $p=8.5\text{m}$  and  $Q=2.5\text{m/s}^2$  & t is measured in seconds. The instantaneous velocity of the object at  $t=2\text{s}$  is
5. A body starts from rest and travels a distance 's' with uniform acceleration, then moves uniformly a distance 2 s and finally comes to rest after moving further 5 s under uniform retardation. The ratio of average velocity to maximum velocity is
6. A balloon rises from rest on the ground with constant acceleration  $1.25\text{m/s}^2$ . A stone is dropped when the balloon has risen to a height of 40 m. The time (ins) taken by the stone to reach the ground is
7. A juggler throws balls in to air. He throws one whenever the previous one is at it higher point. If he throws n balls each second, the height to which each ball will rise is
8. In a car race, car A takes 45 less than car B at the finish and parses the finishing point with a velocity v more than the Car B. Assuming that the car A & B start form rest and travel with constant accelerations  $a_1=4\text{m/s}^2$  respectively, the value of V in m/s is ....
9. A boy standing on a stationary lift (open from above) throws a ball upwards with the maximum initial speed he can, equal to 49 m How much time does the ball take to return to his hands? If the lift starts moving up with a uniform speed of 5 m / s & the throws the ball up with the boy again throws the ball up with the maximum speed he can how long the ball take to return to his hand ?
10. A police van moving on a highway with a speed of  $30\text{kmh}^{-1}$  fires a bullet at a thief's car speeding away in a same direction with a speed of 192 km/h. If the muzzle speed of the buller 150 m/t. A with speed does the bullet hit the thief's car ?
11. In a car race on straight road, car A takes a time t less than car B at the finish and passes finishing point with a speed v more than that of car B. Both the cars start from rest and travel with constant acceleration  $a_1$  and  $a_2$  respectively. Then v is equal to

- 1)  $\frac{a_1 + a_2}{2}t$       2)  $\sqrt{a_1 a_2}t$       3)  $\sqrt{2a_1 a_2}t$       4)  $\frac{2a_1 a_2}{a_1 + a_2}t$

12. A passenger train of length 60 m travels at a speed of 80 km/hr. Another freight train of length 120 m travels at a speed of 30 km/hr. The ratio of times taken by the passenger train to completely cross the freight train when: (i) they are moving in the same direction, and (ii) in the opposite direction is

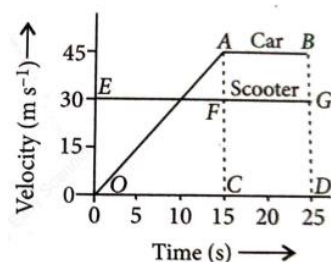
- 1)  $\frac{25}{11}$       2)  $\frac{3}{2}$       3)  $\frac{5}{2}$       4)  $\frac{11}{5}$

13. Which graph corresponds to an object moving with a constant negative acceleration and a positive velocity?



14. The velocity-time graphs of a car and a scooter are shown in the figure.

(i) The difference between the distance travelled by the car and the scooter in 15 s and ii) the time at which the car will catch up with the scooter are, respectively



- 1) 112.5m and 15s      2) 337.5m and 25s      3) 225.5m and 10s      4) 112.5m and 22.5s.

15. A particle is moving with speed  $v = b\sqrt{x}$  along positive x-axis. Calculate the speed of the particle at time  $t = \tau$  (assume that the particle is at origin at  $t=0$ )

- 1)  $b^2\tau$       2)  $\frac{b^2\tau}{2}$       3)  $\frac{b^2\tau}{\sqrt{2}}$       4)  $\frac{b^2\tau}{4}$

16. The position of a particle as a function of time  $t$ , is given by  $x(t) = at + bt^2 - ct^3$  where  $a$ ,  $b$  and  $c$  are constants. When the particle attains zero acceleration, then its velocity will be

- 1)  $a + \frac{b^2}{4c}$       2)  $a + \frac{b^2}{3c}$       3)  $a + \frac{b^2}{c}$       4)  $a + \frac{b^2}{2c}$

17. A body moving with some initial velocity and having uniform acceleration attains a final velocity  $v$  m/s after travelling  $x$  m. If its final velocity is  $v = \sqrt{180 - 7x}$ , find the acceleration of the body.

- 1)  $-3.5\text{m/s}^2$       2)  $-7\text{m/s}^2$       3)  $-15\text{m/s}^2$       4)  $-30\text{m/s}^2$

18. A body initially at rest is moving with uniform acceleration  $a$ . Its velocity after  $n$  seconds is  $v$ . The displacement of the body in last 2s is

- 1)  $\frac{2v(n-1)}{n}$       2)  $\frac{v(n-1)}{n}$       3)  $\frac{v(n+1)}{n}$       4)  $\frac{2v(n+1)}{n}$

19. A ball A is thrown vertically upwards with speed  $u$ . At the same instant another ball B is released from rest at height  $h$ . At time  $t$ , the speed of A relative to B is

- 1)  $u$       2)  $u - 2gt$       3)  $\sqrt{u^2 - 2gh}$       4)  $u - gt$

20. A bullet fired into a wooden block loses half of its velocity after penetrating 40 cm. It comes to rest after penetrating a further distance of

- 1)  $\frac{22}{3}$  cm      2)  $\frac{40}{3}$  cm      3)  $\frac{20}{3}$  cm      4)  $\frac{22}{5}$  cm

21. A particle is released from rest from a tower of height  $3h$ . The ratio of the intervals of time to cover three equal heights  $h$  is

- 1)  $t_1 : t_2 : t_3 = 3 : 2 : 1$       2)  $t_1 : t_2 : t_3 = 1 : (\sqrt{2} - 1) : (\sqrt{3} - 2)$   
 3)  $t_1 : t_2 : t_3 = \sqrt{3} : \sqrt{2} : 1$       4)  $t_1 : t_2 : t_3 = 1 : (\sqrt{2} - 1) : (\sqrt{3} - \sqrt{2})$

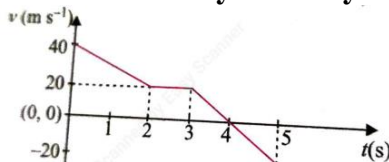
22. It is a common observation that rain clouds can be at about 1 km altitude above the ground. If a rain drop falls from such a height freely under gravity, then what will be its speed in  $\text{kmh}^{-1}$ ? (Take  $g = 10 \text{ m s}^{-2}$ )

- 1) 510      2) 610      3) 710      4) 910

23. A stone is dropped from the top of a tall cliff and  $n$  seconds later another stone is thrown vertically downwards with a velocity  $u$ . Then the second stone overtakes the first, below the top of the cliff at a distance given by

- 1)  $\frac{g}{2} \left[ \frac{n \left( u - \frac{gn}{2} \right)}{(u - gn)} \right]^2$       2)  $\frac{g}{2} \left[ \frac{n \left( \frac{u}{2} - gn \right)}{(u - gn)} \right]^2$       3)  $\frac{g}{2} \left[ \frac{n \left( \frac{u}{2} - gn \right)}{\left( \frac{u}{2} - gn \right)} \right]^2$       4)  $\frac{g}{5} \left[ \frac{(u - gn)}{\left( \frac{u}{2} - gn \right)} \right]^2$

24. In the given  $v$ - $t$  graph the distance travelled by the body in 5 seconds will be



- 1) 100 m      2) 80 m      3) 40 m      4) 20 m

25. The motion of a body is given by the equation  $\frac{dv}{dt} = 6 - 3v$  where  $v$  is the speed in  $\text{ms}^{-1}$  and  $t$  is time in s. The body is at rest at  $t=0$ . The speed varies with time as

- 1)  $v = (1 - e^{-3t})$       2)  $v = 2(1 - e^{-3t})$       3)  $v = (1 + e^{-2t})$       4)  $v = 2(1 + e^{-2t})$

26. A cyclist moving on a circular track of radius 40 m completes half a revolution in 40 s. Its average velocity is

- 1) Zero      2)  $4\pi \text{ms}^{-1}$       3)  $2\text{s}^{-1}$       4)  $8\pi \text{ms}^{-1}$

27. A particle moving with uniform acceleration has average velocities  $v_1$ ,  $v_2$  and  $v_3$  over the successive intervals of time  $t_1$ ,  $t_2$  and  $t_3$  respectively. The value of  $\frac{(v_1 - v_2)}{(v_2 - v_3)}$  will be

- 1)  $\frac{t_1 - t_2}{t_2 - t_3}$       2)  $\frac{t_1 - t_2}{t_2 + t_3}$       3)  $\frac{t_1 + t_2}{t_2 - t_3}$       4)  $\frac{t_1 + t_2}{t_2 + t_3}$

28. A 175 m long train is traveling along a straight track with a velocity  $72 \text{ km}^{-1} \text{h}$ . A bird is flying parallel to the train in the opposite direction with a velocity  $18 \text{ km}^{-1} \text{h}$ . The time taken by the bird to cross the train is

- 1) 35 s      2) 27 s      3) 11.6 s      4) 7s

29. A bus is moving with a speed of  $10 \text{ ms}^{-1}$  on a straight road. A scooterist wishes to overtake the scooterist with what speed should the scooterist chase the bus?

- 1)  $40 \text{ ms}^{-1}$       2)  $25 \text{ ms}^{-1}$       3)  $10 \text{ ms}^{-1}$       4)  $20 \text{ ms}^{-1}$

30. On a long horizontally  $9 \text{ kmh}^{-1}$  (with respect to the belt) an drown his father and mother located 50 m apart on the moving belt. The belt moves with a speed of  $4 \text{ kmh}^{-1}$ . For an observer on a stationary platform, the speed of the child running in the direction of motion of the belt is

- 1)  $4 \text{ kmh}^{-1}$       2)  $5 \text{ kmh}^{-1}$       3)  $9 \text{ kmh}^{-1}$       4)  $13 \text{ kmh}^{-1}$

## KEY PHYSICS

1) <b>11.425</b>	2) <b>1250</b>	3) <b>– 1000km/h</b>	4) <b>10m/ss</b>	5) <b>4/7</b>	6) <b>4s</b>	7) <b>g/2n<sup>2</sup></b>	8) <b>8</b>	9) <b>10s,10s</b>	10) <b>105m/s</b>
11) <b>2</b>	12) <b>4</b>	13) <b>1</b>	14) <b>4</b>	15) <b>2</b>	16) <b>1</b>	17) <b>1</b>	18) <b>1</b>	19) <b>1</b>	20) <b>2</b>
21) <b>4</b>	22) <b>1</b>	23) <b>1</b>	24) <b>1</b>	25) <b>2</b>	26) <b>3</b>	27) <b>4</b>	28) <b>4</b>	29) <b>4</b>	30) <b>4</b>

## SOLUTION

1.  $u = 252 \text{ km/h} = 252 \times \frac{5}{18} = 70 \text{ m/s}$

$$s = 400 \text{ m} \text{ and } v = 0$$

$$v^2 - u^2 = 2as$$

$$a = \frac{-u^2}{2 \times s} = \frac{-70 \times 70}{2 \times 400} = -6.125$$

$$v = u + at$$

$$t = \frac{-u}{a} = \frac{-70}{-6.125} = 11.42 \text{ s}$$

2.  $s = ut + \frac{1}{2}at^2$

Train A:

$$u = 72 \text{ km/h} = 20 \text{ m/s}$$

$$t = 50 \text{ s}$$

$$a_1 = 0$$

$$s_1 = ut + \frac{1}{2}at^2 = 1000 \text{ m}$$

Train B:

$$s = ut + \frac{1}{2}at^2$$

$$= 20 \times 50 + \frac{1}{2} \times 1 \times 50^2$$

$$= 2250$$

$$\text{original distance } 2250 - 1000 = 1250 \text{ m}$$

3.  $v_{jet} = 1500 \text{ km/h}^{-1}$

$$V = -2500 \text{ km/h}$$

$$V = V' - v_j e$$

$$N' = -1000 \text{ km/h}$$

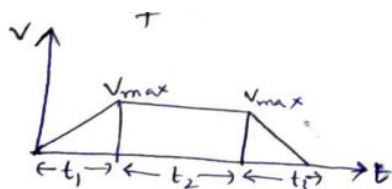
4.

$$x = p + at^2$$

$$v = \frac{dx}{dt} = \frac{d}{dt}(p + at^2) = 2at$$

$$t = 2 \text{ s} : v = 2(2.5)(2) = 10 \text{ m/s}$$

5.



$$s = \frac{1}{2} v_{\max} t_1 \quad t_1 = \frac{2s}{v_{\max}}$$

$$2s = v_{\max} t_2 \quad t_2 = \frac{2s}{v_{\max}}$$

$$3s = \frac{1}{2} v_{\max} \cdot t_3$$

$$t_3 = \frac{10s}{v_{\max}}$$

$$V_{\text{av}} = \frac{\text{Total distance}}{\text{Total time}} = \frac{s + 2s + 5s}{\frac{2s}{v_{\max}} + \frac{2s}{v_{\max}} + \frac{10s}{v_{\max}}}$$

$$\frac{V_{\text{avg}}}{v_{\max}} = \frac{8s}{14s} = \frac{4}{7}$$

6. 
$$h = \frac{1}{2} at^2$$

$$t = \sqrt{\frac{2h}{a}} = \sqrt{\frac{2 \times 40 \times 8}{10}} = 8$$

$$\text{velocity after } 8\text{s} \quad v = 0 + \frac{10}{8} \times 8 = 10\text{m/s}$$

$$\text{For stone } -40 = +10t - \frac{1}{2} \times 10t^2$$

$$10t^2 - 2 \times 10t - 2 \times 40 = 0$$

$$t^2 - 2t - 8 = 0$$

$$t^2 - 4t + 2t - 8 = 0 \quad t = 45$$

 7. Time taken by each ball to reach highest point  $t = 1/n$  second.

 As the juggler throws the second ball, when the first ball is at its highest point so  $v=0$ 

$$v = u + at$$

$$0 = u + (-9) \frac{1}{n} \Rightarrow u = 9/n$$

$$v^2 - u^2 + 2as = 0$$

$$\text{Also } 0 = 9/n^2 + 2(-g)h$$

$$h = \frac{9}{2n^2}$$

8. 
$$t_1 = t_2 - t$$

$$v_1 = v_2 + v$$

$$s = \frac{1}{2} a_1 t_1^2$$

$$s = \frac{1}{2} a_2 t_2^2$$

$$v_1 = a_1 t_1$$

$$v_2 = a_2 t_2 \Rightarrow v_2 + v = a_1 t_1$$

$$a_2 t_2 + v = a_1 t_1 \Rightarrow t_2 = \frac{v + a_1 t_1}{a_1 - a_2}$$

$$\sqrt{\frac{ag}{a_1}} = \frac{t_1}{t_2} = 1 - \frac{t}{t_2} \Rightarrow \sqrt{\frac{a_2}{a_1}} = 1 - \frac{t(a_1 - a_2)}{v + a_1 t}$$

$$\frac{\sqrt{av}}{\sqrt{a_1}} = \frac{v + a_2 t}{v + a_1 t}$$

$$v = \frac{(a_1 \sqrt{a_2} - a_2 \sqrt{a_1}) t}{(\sqrt{a_1} - \sqrt{a_2})} = 8 \text{ m/s}$$

9.

1)

$$s = 0 \quad u = 4 \text{ amls} \quad a = -9$$

$$s = ut + \frac{1}{2} at^2$$

$$t = \frac{-2u}{a} = 10 \text{ s}$$

2)

$$s = ut + \frac{1}{2} at^2$$

$$5t = 54t + \frac{1}{2} (-9)t^2$$

$$t = \frac{2 \times 49}{9.8} = 10 \text{ s}$$

10.  $v_v = 30 \text{ km/h} = \frac{25}{3} \text{ m/s}$

$$V_{BV} = V_{BG} - V_{VG}$$

$$V_{BG} = V_{BV} + V_{VG}$$

$$= \left( 150 + \frac{25}{3} \right) \text{ m/s} = \frac{475}{3} \text{ m/s}$$

$$v_T = 195 \times \frac{5}{18} = \frac{160}{3} \text{ m/s}$$

$$V_{BT} = V_{BG} - V_{TG}$$

$$= \left( \frac{475}{3} - \frac{160}{3} \right) \text{ m/s}$$

$$= 105 \text{ m/s.}$$

11. Both cars cover same distance.

$$\frac{1}{2} a_1 t_1^2 = \frac{1}{2} a_2 t_2^2$$

$$\text{Also, } t_2 - t_1 = t$$

$$a_1 t_1 = v + a_2 t_2$$

From eqn. (i) and (ii),

$$\left( \frac{a_1}{a_2} \right) = \left( \frac{t + t_1}{t_1} \right)^2 = \left( \frac{t}{t_1} + 1 \right)^2 \text{ or } \frac{t}{t_1} + 1 = \sqrt{\frac{a_1}{a_2}}; t_1 = \frac{\sqrt{a_2}}{\sqrt{a_1} - \sqrt{a_2}} t$$

From eqn. (ii) and (iii),

$$a_1 t_1 = v + a_2(t + t_1); v + a_2 t = (a_1 - a_2)t_1$$

$$\text{or } v + a_2 t = (a_1 - a_2) \times \frac{\sqrt{a_2 t}}{(\sqrt{a_1} - \sqrt{a_2})}$$

$$v + a_2 t = \sqrt{a_1 a_2} t + a_2 t \quad \therefore v = \sqrt{a_1 a_2} t$$

12.  $60 + 120 = 180 \text{ m}$

$$60 + 120 =$$

$$\text{velocity is } v_1 - v_2 = 80 - 30 = 50 \text{ kmh}^{-1}$$

So time taken to cross each other,

$$t_1 = \frac{180}{50 \times \frac{10^3}{3600}} = \frac{18 \times 18}{25} \text{ s}$$

when the trains are moving in opposite direction, relative velocity,  $|v_1 - (-v_2)| = 80 + 30 = 110 \text{ kmh}^{-1}$

So, time taken to cross each other

$$t_2 = \frac{180}{110 \times \frac{1000}{3600}} = \frac{18 \times 36}{110} \text{ s}; \text{ Ratio } \frac{t_1}{t_2} = \frac{\frac{18 \times 18}{25}}{\frac{18 \times 36}{110}} = \frac{11}{5}$$

13. Here, acceleration is given by,  $a = -c$

$$\frac{dv}{dt} = -c \text{ or } \frac{dx}{dt} \cdot \frac{dv}{dx} = -c; v dv = -c dx$$

$$\frac{v^2}{2} = -cx + k \text{ or } x = -\frac{v^2}{2c} + \frac{k}{c}$$

From this equation, we conclude option (a) is correct

14. Distance travelled by car in 15 s

$$= \frac{1}{2} \times AC \times OC = \frac{1}{2} (45)(15) = \frac{675}{2} \text{ m}$$

$$\text{Distance travelled by scooter in } 15 \text{ s} = v \times t = 30 \times 15 = 450,$$

$$\text{Required difference in distance} = 450 - \frac{675}{2} = \frac{225}{2} = 112.5 \text{ m}$$

$$\text{Let car catches scooter in time } t, \frac{675}{2} + 45(t - 15) = 30t$$

$$337.5 + 45t - 675 = 30t \Rightarrow 15t = 337.5 \Rightarrow t = 22.5 \text{ s}$$

15. Given velocity as a function of x i.e.,  $v = b\sqrt{x}$  Differentiating w.r.t. time, we get

$$\frac{dv}{dt} = \frac{b}{2\sqrt{x}} \frac{dx}{dt} \Rightarrow a = \frac{bv}{2\sqrt{x}}$$

$$a = \frac{b(b\sqrt{x})}{2\sqrt{x}} \quad (\because v = b\sqrt{x})$$

$$a = \frac{b^2}{2}$$

$$\text{Again, } a = \frac{dv}{dt} = \frac{b^2}{2} \quad \therefore v = \frac{b^2}{2} t \Rightarrow (v)_{t=\tau} = \frac{b^2}{2} \tau$$

16. Here  $x(t) = at + bt^2 - ct^3$

$$\therefore v(t) = \frac{dx(t)}{dt} = a + 2bt - 3ct^2; a(t) = \frac{dv(t)}{dt} = 2b - 6ct$$

$$\therefore a(t) = 0 \Rightarrow 2b - 6ct = 0 \Rightarrow t = 2b / 6c$$

$$\therefore v = a + 2b\left(\frac{2b}{6c}\right) - 3c\left(\frac{2b}{6c}\right)^2 = a + \frac{b^2}{3c}$$

17.  $v = \sqrt{180 - 7x}$  where  $x$  is the distance.

$$\therefore v^2 = 180 - 7x$$

From the dimensions, 180 has dimensions of square of velocity. For a body travelling with uniform acceleration,

$$v^2 - u^2 = 2aS \text{ is valid. By inspection one can say}$$

$$u^2 = 180, 2aS = -7x \text{ (here } S = x)$$

$$-7x = 2ax. \therefore a = -3.5 \text{ m/s}^2$$

18. Here,  $a = \frac{v-u}{t} = \frac{v-0}{n} = \frac{v}{n}$

Displacement in last  $2s$

$$S_n - S_{n-2} = \frac{1}{2}an^2 - \frac{1}{2}a(n-2)^2$$

$$= 2a(n-1) = 2\frac{v}{n}(n-1) = \frac{2v(n-1)}{n}$$

19. Taking upwards motion of ball A for time  $t$ , in velocity is  $V_A = u - gt$

Taking downwards motion of ball B for time  $t$ , its velocity is  $V_B = gt$

Relative velocity of A w.r.t B

$$= v_{AB} = v_A - (-v_B) = (u - gt) - (-gt) = u$$

20. For first part of penetration, by equation of motion

$$\left(\frac{u}{2}\right)^2 - (u)^2 = 2aS \text{ or } a = -\frac{3u^2}{8S}$$

For later part of penetration

$$(0)^2 - \left(\frac{u}{2}\right)^2 = 2aS' \text{ or } S' = -\frac{u^2}{8a}$$

$$S' = -\frac{u^2}{8\left(-\frac{3u^2}{8S}\right)} \text{ (Using (i))}$$

$$S' = \frac{S}{3} = \frac{40}{3} \text{ cm } (\because S = 40 \text{ cm given})$$

21. Let  $t_1, t_2, t_3$  be the timings for three heights  $h$  covered during the free fall of the successive e

$$h = \frac{1}{2}gt_1^2 \text{ or } t_1 = \sqrt{\frac{2h}{g}} \text{ } (\because u = 0) \quad \dots(i)$$

$$2h = \frac{1}{2}g(t_1 + t_2)^2 \text{ or } t_1 + t_2 = \sqrt{\frac{4h}{g}} \quad \dots(ii)$$

$$3h = \frac{1}{2}g(t_1 + t_2 + t_3)^2 \text{ or } t_1 + t_2 + t_3 = \sqrt{\frac{6h}{g}} \quad \dots(iii)$$

Subtracting (i) from (ii), we get

$$t_2 = \sqrt{\frac{4h}{g}} - \sqrt{\frac{2h}{g}} = \sqrt{\frac{2h}{g}}(\sqrt{2} - 1)$$

Subtracting (ii) from (iii), we get



$$t_3 = \sqrt{\frac{6h}{g}} - \sqrt{\frac{4h}{g}} = \sqrt{\frac{2h}{g}}(\sqrt{3} - \sqrt{2})$$

From (i), (iv) and (v), we get

$$t_1 : t_2 : t_3 = 1 : (\sqrt{2} - 1) : (\sqrt{3} - \sqrt{2})$$

22. Here,  $u = 0, g = 10\text{ms}^{-2}, h = 1\text{km} = 1000\text{m}$

$$Asv^2 - u^2 = 2gh \quad \therefore v^2 = 2gh$$

$$orv = \sqrt{2gh} = \sqrt{2 \times 10 \times 1000} = 100\sqrt{2}\text{ms}^{-1}$$

$$= 100\sqrt{2} \times \frac{18}{5} \text{kmh}^{-1} = 360\sqrt{2}\text{kmh}^{-1} \approx 510\text{kmh}^{-1}$$

23. Let the two stones meet at time  $t$  For the first stone,

$$S_1 = \frac{1}{2}gt^2 \quad (\because u = 0)$$

For the second stone,

$$S_2 = u(t-n) + \frac{1}{2}g(t-n)^2 \quad \dots(ii)$$

Displacement is same  $\therefore S_1 = S_2$

$$\frac{1}{2}gt^2 = u(t-n) + \frac{1}{2}g(t-n)^2 \quad (\text{Using (i) and (ii)})$$

$$\frac{1}{2}gt^2 = ut - nu + \frac{1}{2}gt^2 + \frac{1}{2}gn^2 - gtn$$

$$ut - gtn = nu - \frac{1}{2}gn^2$$

$$t = \frac{nu - \frac{1}{2}gn^2}{u - gn} = \frac{n\left(u - \frac{g}{2}n\right)}{u - gn}; \therefore S_1 = \frac{g}{2} \left[ \frac{n\left(u - \frac{g}{2}n\right)}{(u - gn)} \right]^2 \quad [\text{from (i)}]$$

24. The distance is equal to total area under  $v-t$  graph

$$= \frac{20 \times 2}{2} + 20 \times 2 + 20 \times 1 + \frac{20 \times 1}{2} + \frac{20 \times 1}{2} = 100\text{m}$$

25.  $\frac{dv}{dt} = 6 - 3v \implies \int \frac{dv}{6 - 3v} = \int dt$

Integrating both sides, we get,  $t = -\frac{1}{3} \ln(6 - 3v) + C$

where  $C$  is a constant of integration

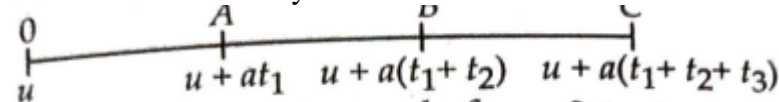
$$\text{At } t = 0, v = 0 \quad \therefore C = \frac{1}{3} \ln 6$$

$$\therefore t = -\frac{1}{3} \ln \left( \frac{6 - 3v}{6} \right) \text{ or } e^{-3t} = 1 - \frac{1}{2}v \text{ or } v = 2(1 - e^{-3t})$$

26. Average velocity

$$= \frac{\text{Displacement}}{\text{Time taken}} = \frac{2R}{t} = \frac{2 \times 40}{40} = 2\text{ms}^{-1}$$

27. Let  $u$  be initial velocity and  $a$  be uniform acceleration



Average velocities in the intervals from 0 to  $t_1$ ,  $t_1$  to  $t_2$  and to  $t_3$  are

$$v_1 = \frac{u + u + at_1}{2} = u + \frac{a}{2}t_1$$

$$v_2 = \frac{u + at_1 + u + a(t_1 + t_2)}{2} = u + at_1 + \frac{a}{2}t_2$$

$$v_3 = \frac{u + a(t_1 + t_2) + u + a(t_1 + t_2 + t_3)}{2} = u + at_1 + at_2 + \frac{a}{2}t_3$$

Subtract (i) from (ii), we get

$$v_2 - v_1 = \frac{a}{2}(t_1 + t_2)$$

Subtract (ii) from (iii), we get

$$v_3 - v_2 = \frac{a}{2}(t_2 + t_3)$$

Divide (iv) by (v), we get

$$\frac{v_2 - v_1}{v_3 - v_2} = \frac{(t_1 + t_2)}{(t_2 + t_3)} \text{ or } \frac{v_1 - v_2}{v_2 - v_3} = \frac{(t_1 + t_2)}{(t_2 + t_3)}$$

28. Velocity of train,

$$v_T = 72 \text{ km/h} = 72 \times \frac{5}{18} \text{ m/s} = 20 \text{ m/s}$$

$$\text{Velocity of bird, } v_B = 18 \text{ km/h} = 18 \times \frac{5}{18} \text{ m/s} = 5 \text{ m/s}$$

Since bird is flying parallel to train in opposite direction.

Relative velocity of bird w.r.t. train =  $v_B + v_T = 25 \text{ m/s}$

Train's length = 175 m

Time taken by the bird to cross the train is =  $175/25 = 7 \text{ s}$

29. Let  $v_s$  be the velocity of scooter. The distance between scooter and the bus = 1 km = 1000m

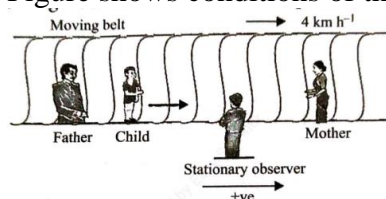
The velocity of bus,  $v_b = 10 \text{ m s}^{-1}$

Time taken to overtake the bus,  $t = 100 \text{ s}$ .

Relative velocity of the scooter w.r.t. the bus =  $(v_s - 10)$

$$t = \frac{1000}{(v_s - 10)} = 100 \text{ or } v_s = 20 \text{ m s}^{-1}$$

30. Figure shows conditions of the question.



In this case,

Speed of belt w.r.t. ground,  $v_{BG} = 4 \text{ kmh}^{-1}$

Speed of child w.r.t. belt,  $v_{CB} = 9 \text{ kmh}^{-1}$

∴ For an observer on a stationary platform, speed of child running in the direction of motion of the belt

$$v_{CG} = v_{CB} + v_{BG} = 9 \text{ kmh}^{-1} + 4 \text{ kmh}^{-1} = 13 \text{ kmh}^{-1}$$